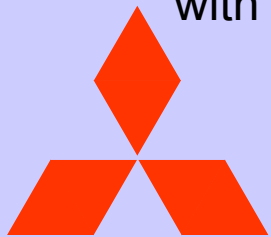


# Coding and Modulation in Cameras



Ramesh Raskar

with Ashok Veeraraghavan, Amit Agrawal, Jack Tumblin, Ankit Mohan



Mitsubishi Electric Research Labs (MERL)

Cambridge, MA

# Overview

- Coded Exposure
  - Motion Deblurring



- Coded Aperture
  - Digital Refocussing
    - Extended depth of field
  - Optical Heterodyning
    - Light Field Capture
    - 4D to 2D mapping





Motion Blurred Input Photo



Approximate rectified crop of photo



Image Deblurred by solving a linear system. No post-processing

# Flutter Shutter Camera

Raskar, Agrawal, Tumblin [Siggraph2006]



Ferroelectric LCD shutter in front of the lens is turned opaque or transparent in a rapid binary sequence

# Coded Exposure Photography: Assisting Motion Deblurring using Fluttered Shutter

Short Exposure

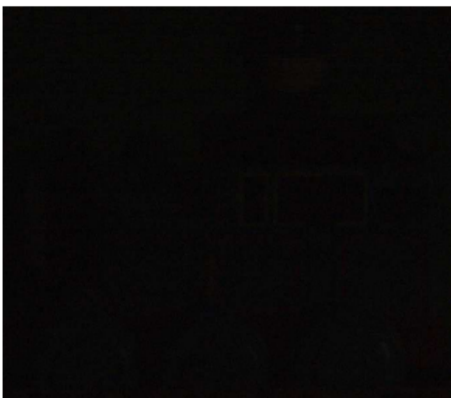
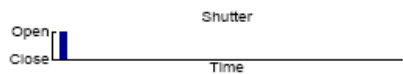
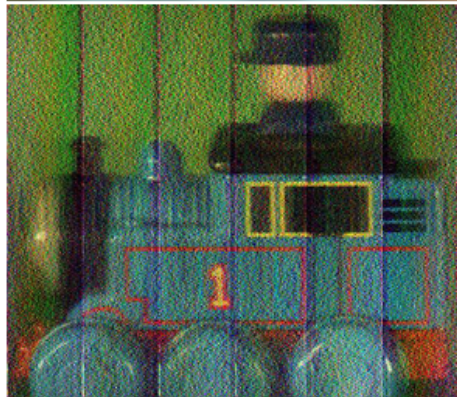
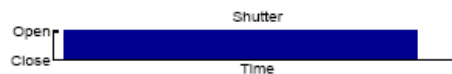


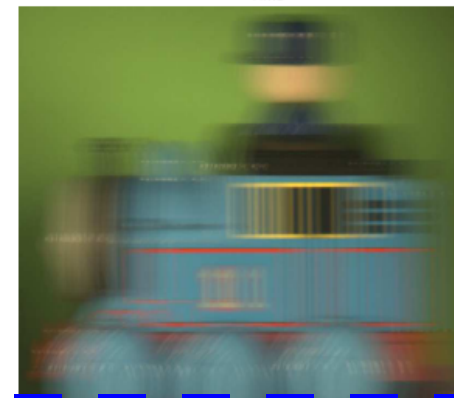
Image is dark and noisy

Traditional



Result has Banding Artifacts and some spatial frequencies are lost

Coded



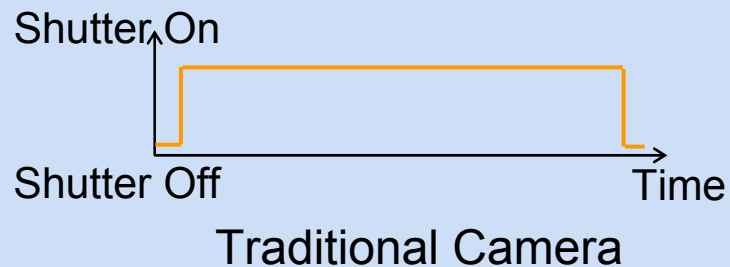
Decoded image is as good as image of a static scene

← Shutter →

← Captured Single Photo →

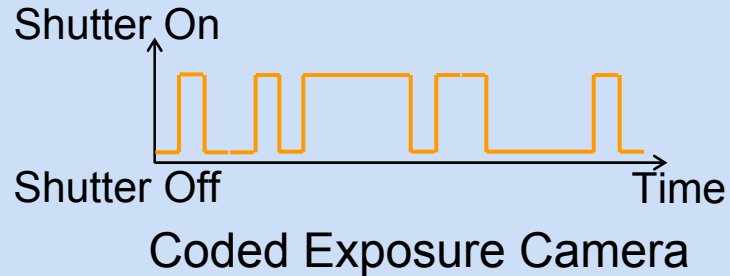
← Deblurred Result →

# Exposure choices for capturing fast moving objects



Keep Shutter open for entire exposure duration

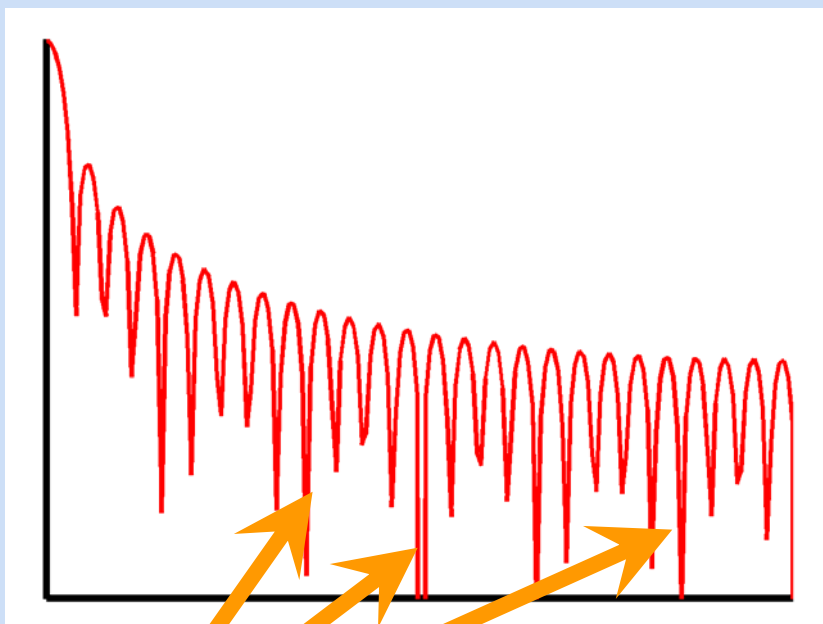
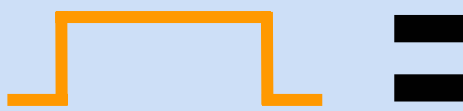
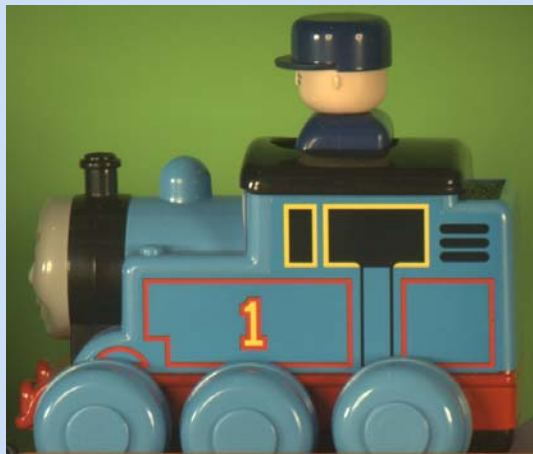
The moving object creates smear



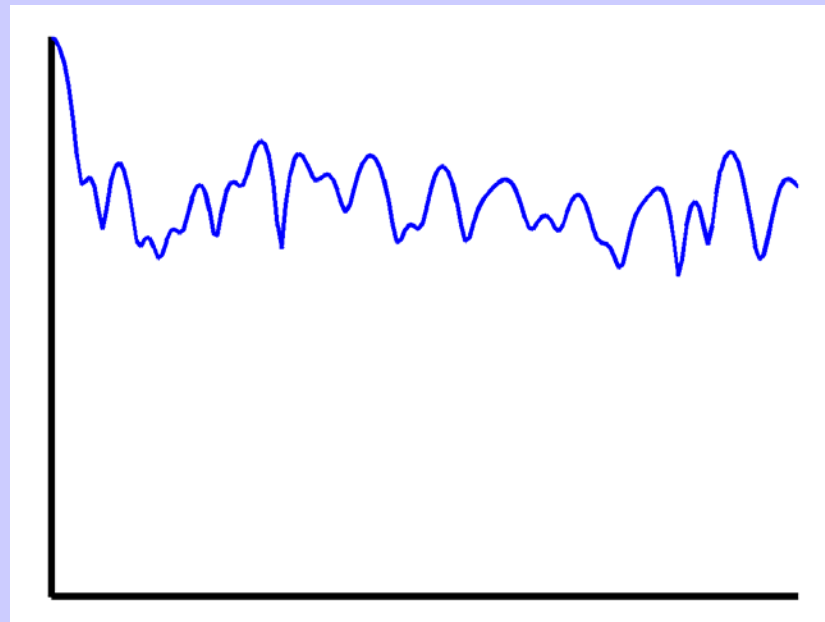
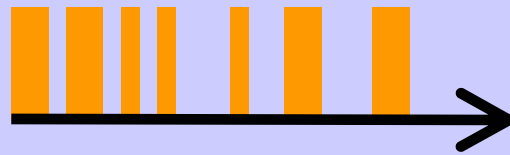
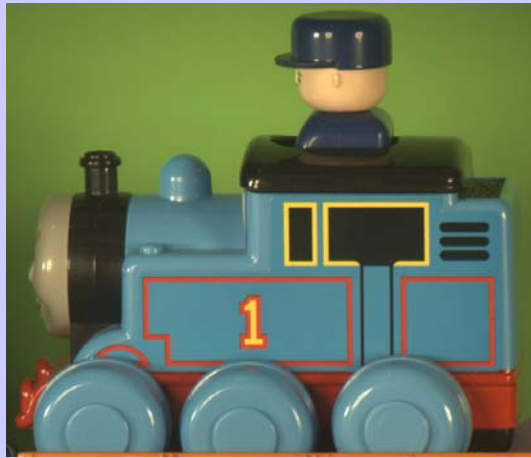
**Flutter shutter** open and closed with a psuedo-random binary sequence within exposure duration to encode the blur



Keep shutter open for very short duration. Avoids blur but image is dark and suffers from noise.

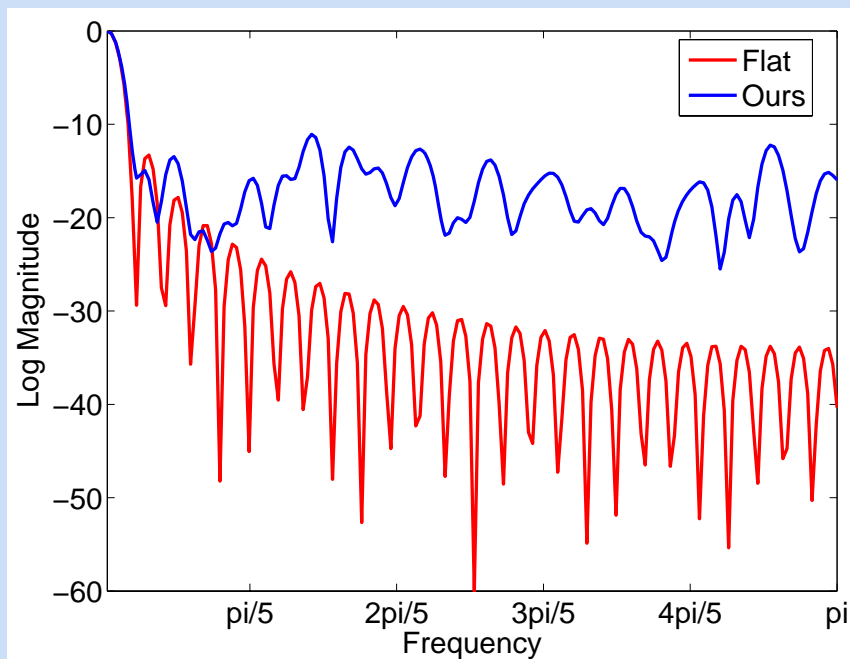




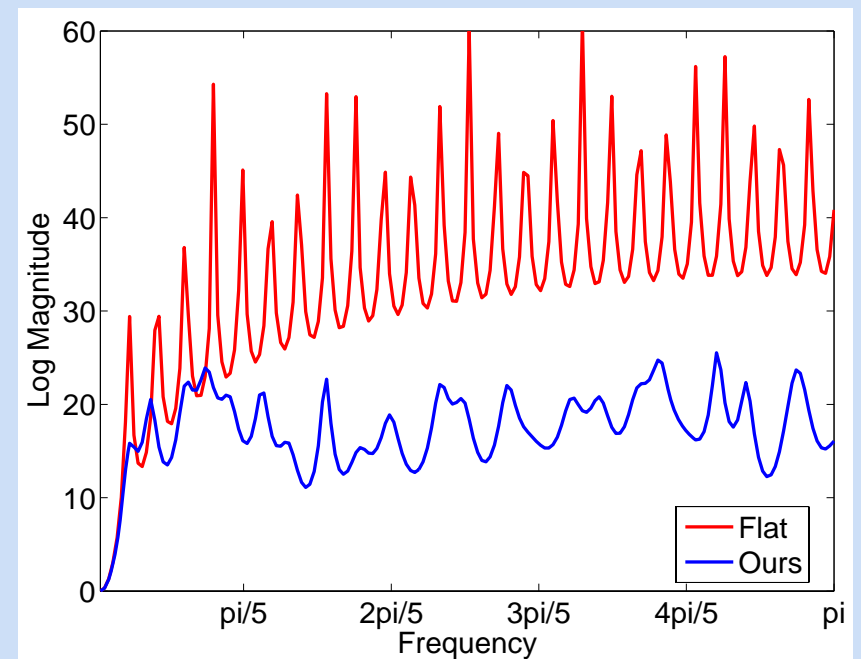


## Coded Motion Blur

- = Preserves high spatial frequencies
- = Deconvolution filter frequency response is nearly flat
- = Deconvolution becomes a well-posed problem



Encoding Filter (Blurring)



Decoding Filter (Deblurring)



# Defocus Blurred Photo



## Digital Refocusing



Refocused Image on Person

# Coded Exposure



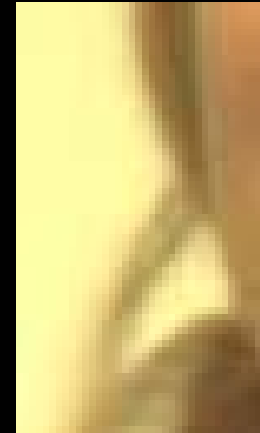
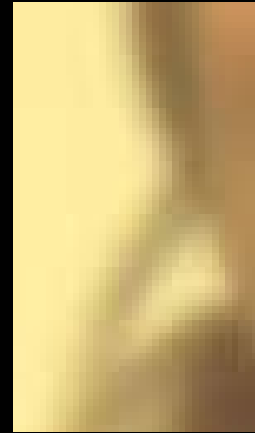
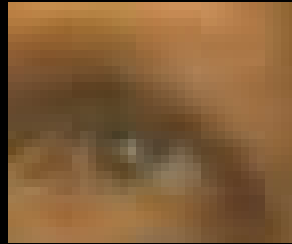
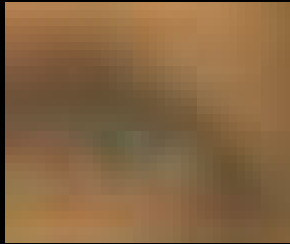
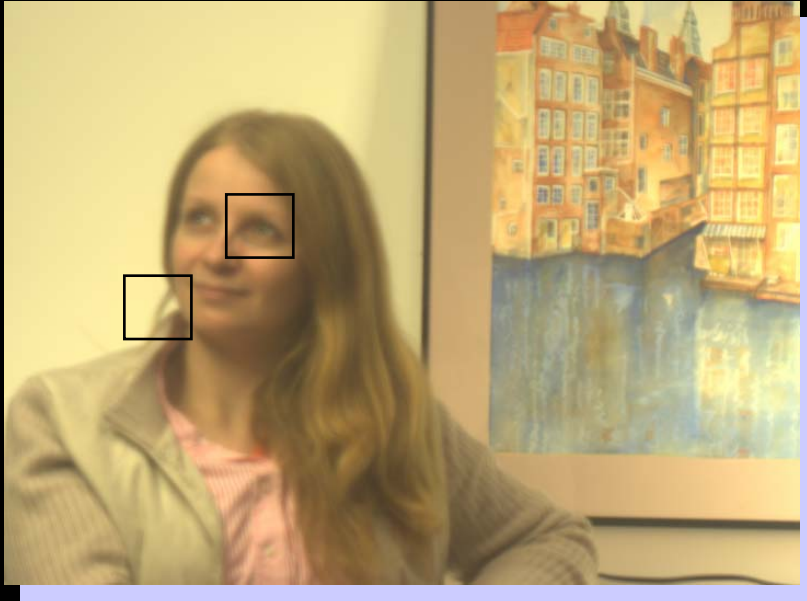
Temporal 1-D  
broadband code

# Coded Aperture



Spatial 2-D  
broadband code

# Digital Refocusing



# Coded Aperture Camera

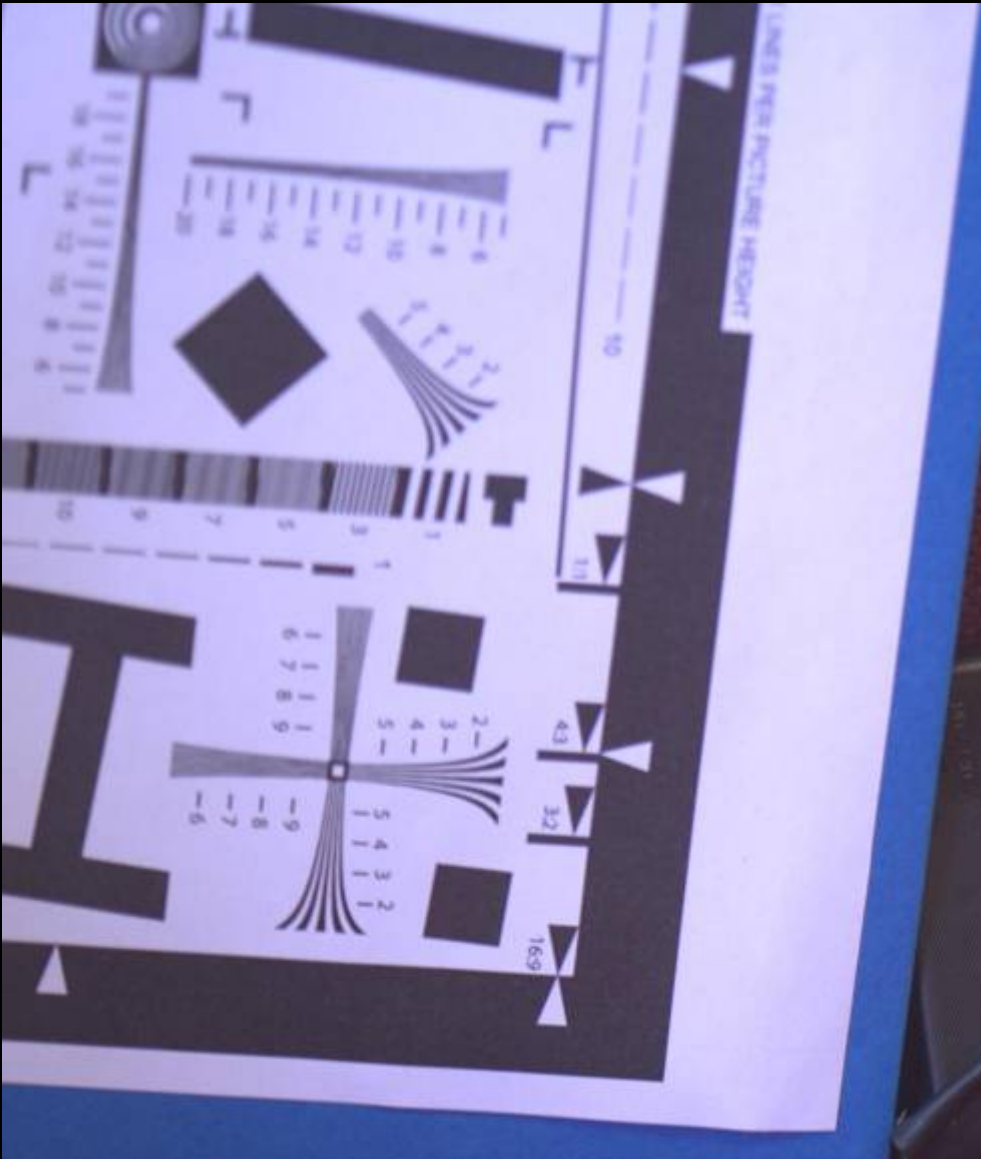


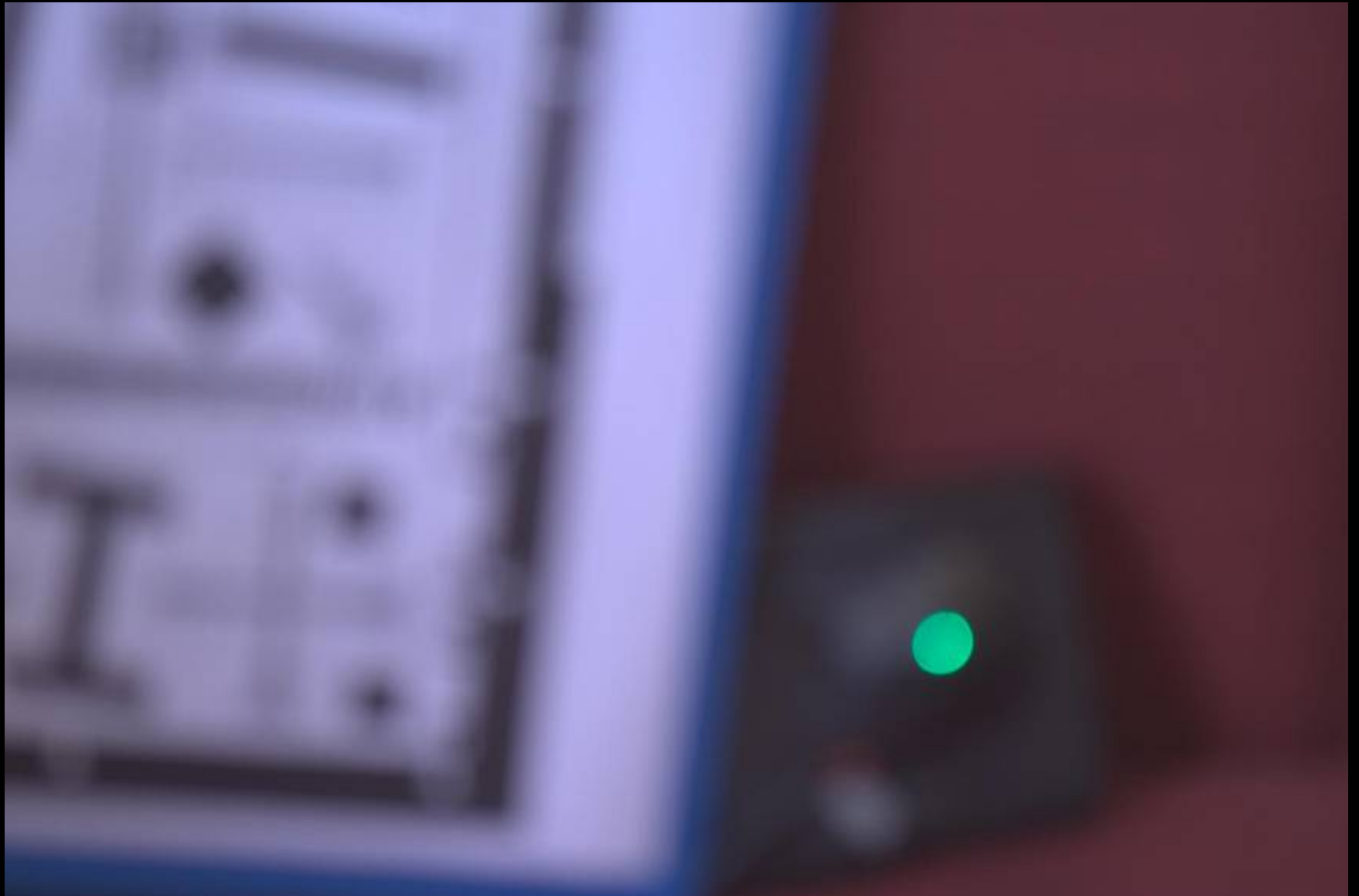
The aperture of a 100 mm lens is modified

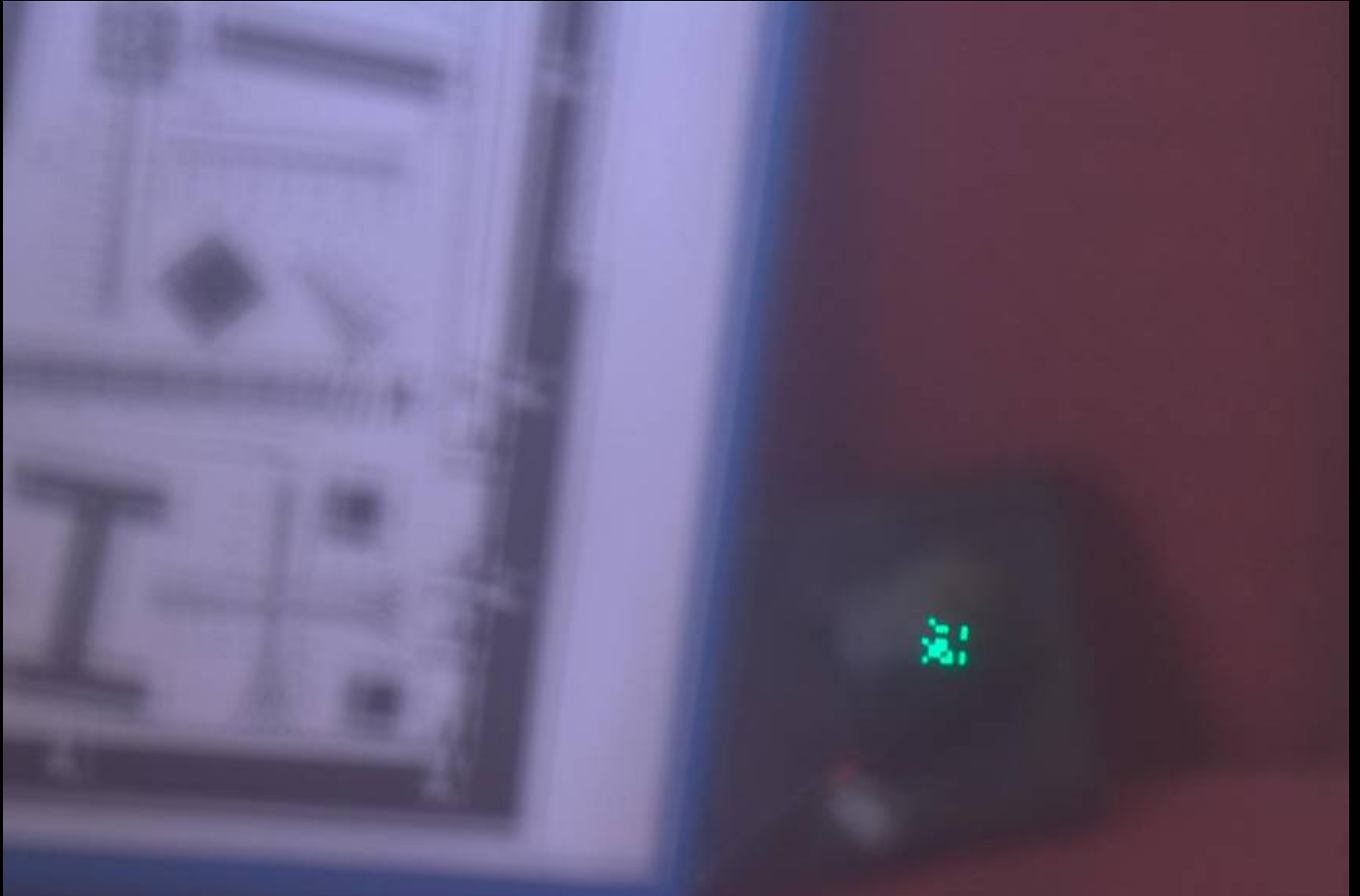
Insert a **coded mask** with chosen binary pattern

Rest of the camera is unmodified









# Comparison with Traditional Camera

Encoded Blur Camera



Traditional Camera



← Captured Blurred Photo →

← Deblurred Image →

## Comparison with Small Aperture Image



Small Aperture  
Image

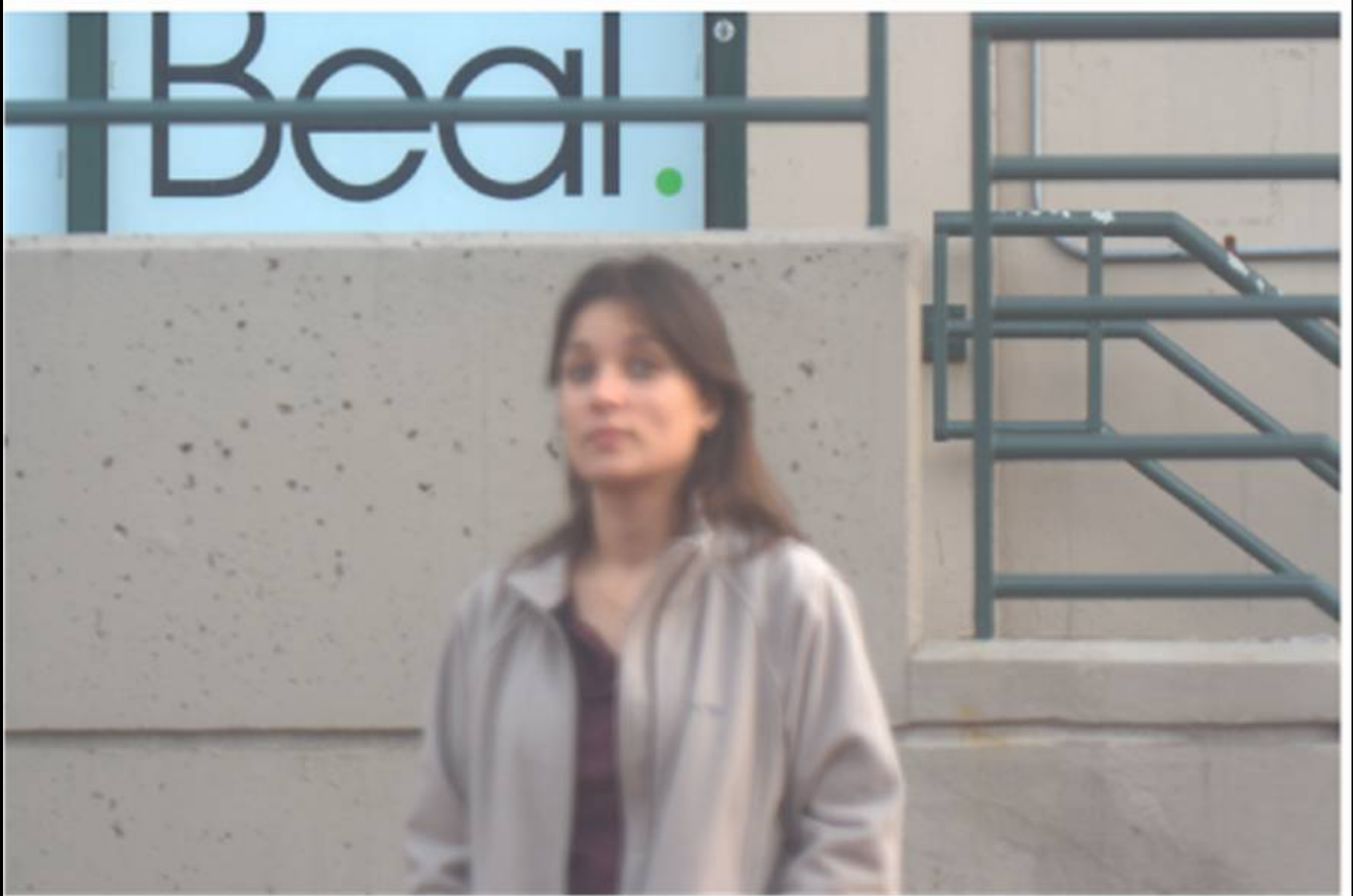


Captured  
Blurred Image



Deblurred  
Image

## Digital Refocusing



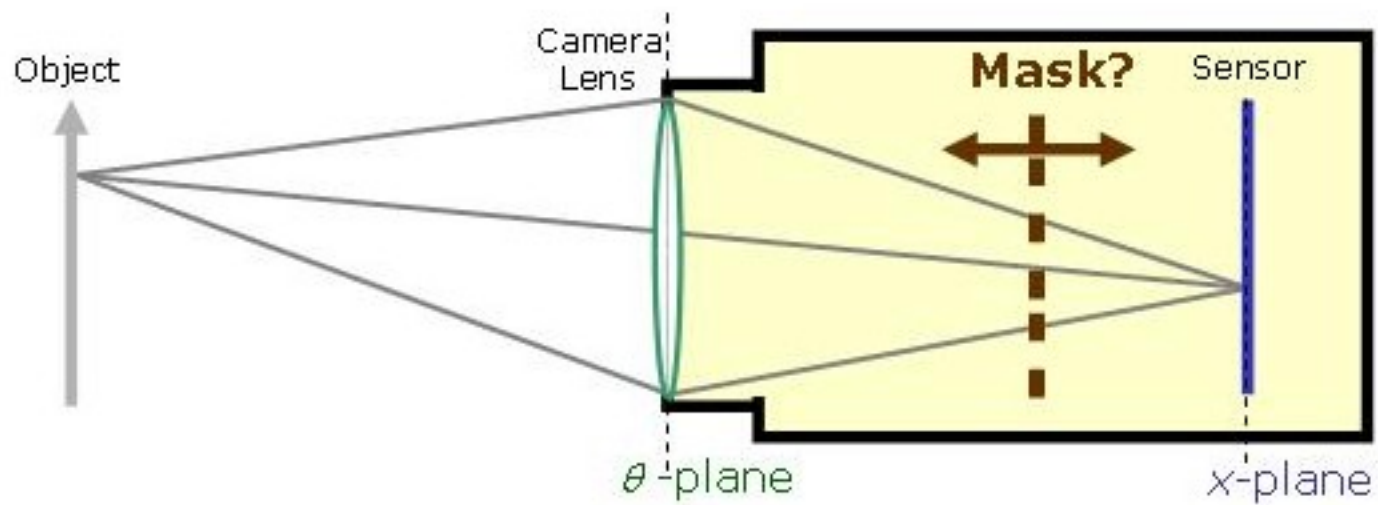
Captured Blurred Image

## Digital Refocusing



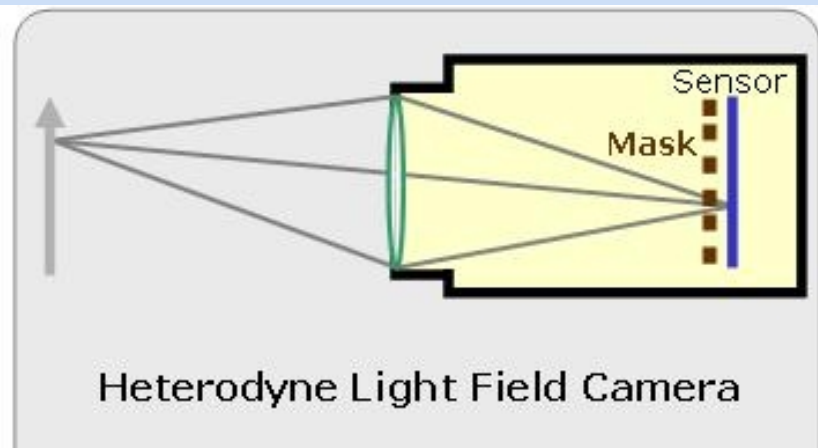
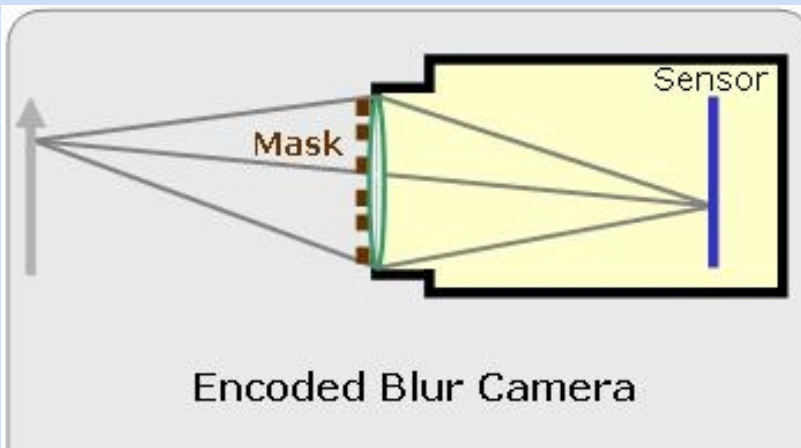
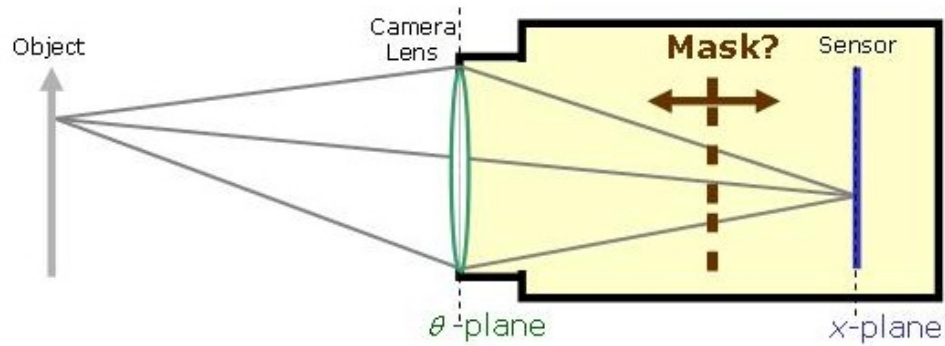
Refocused Image on Person

Can we capture more information by inserting a mask ?

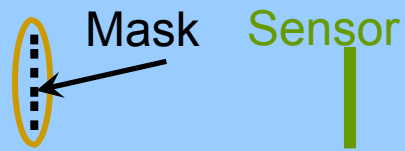
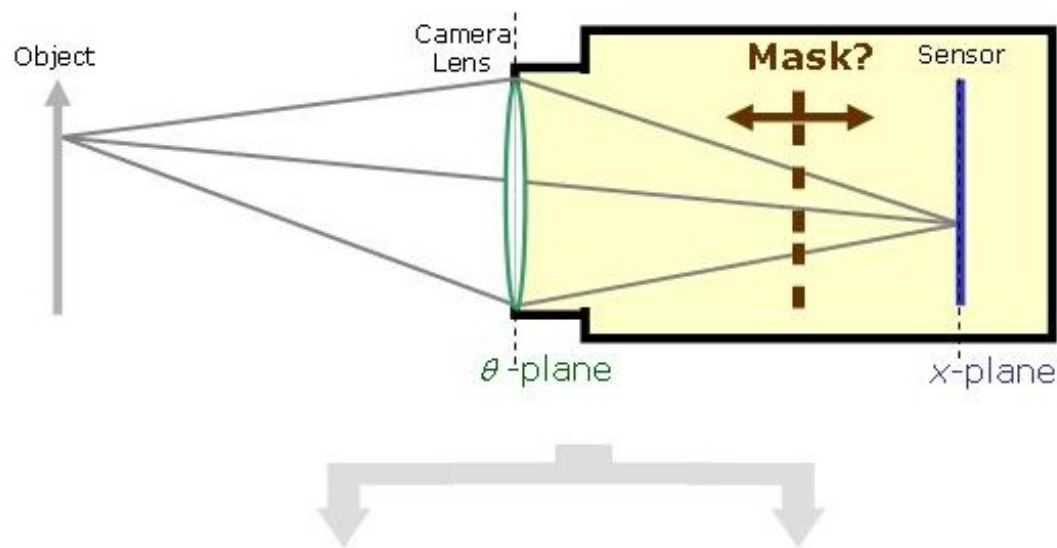




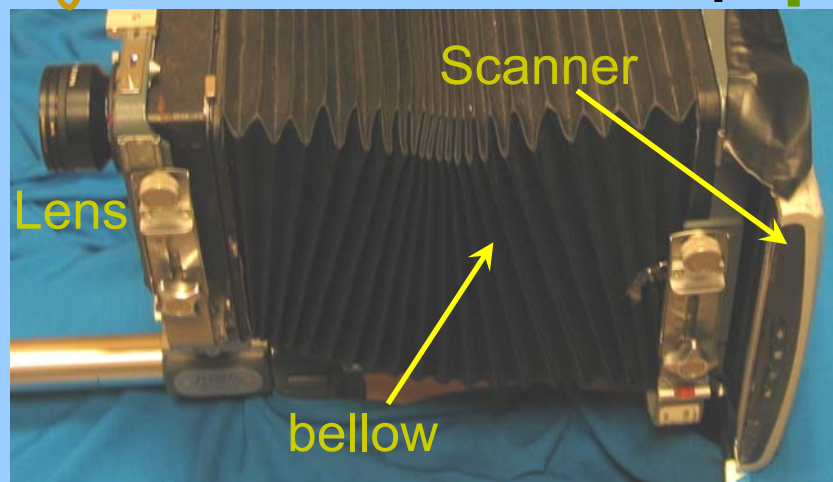
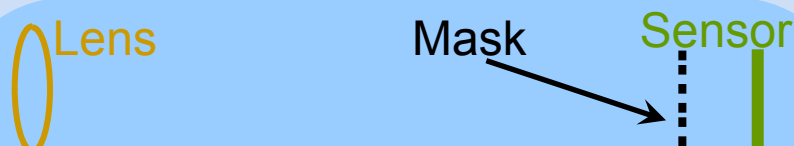
### Coding Light Field Entering a Camera via a Mask



# Coding Light Field Entering a Camera via a Mask

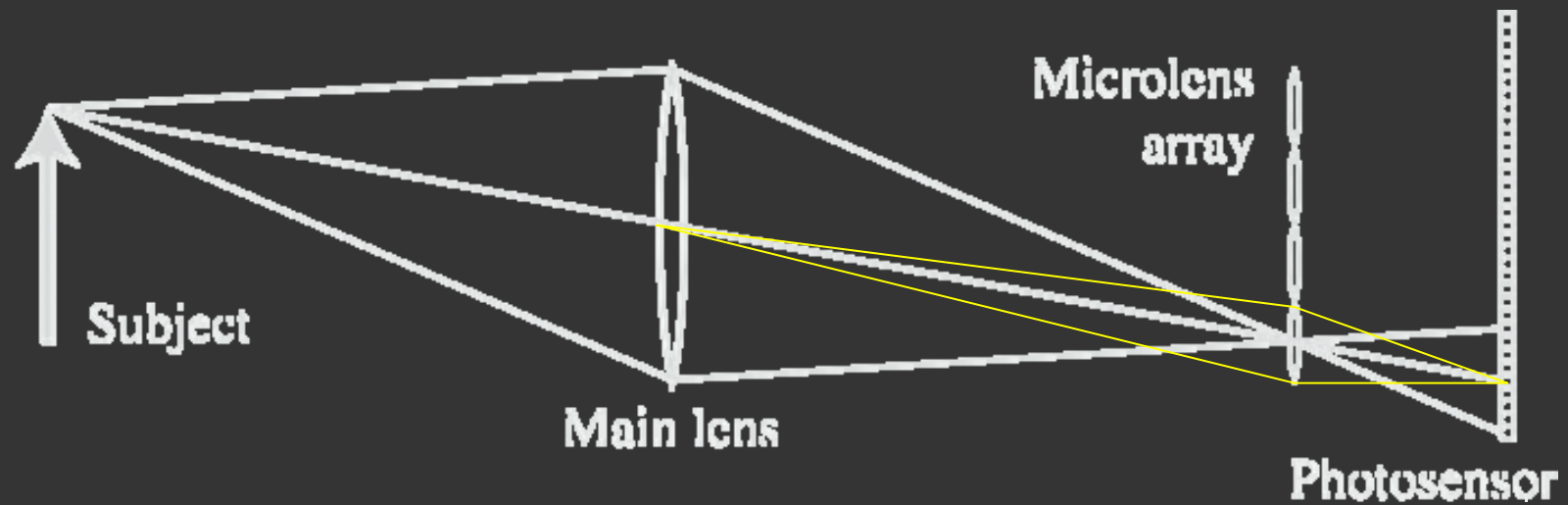
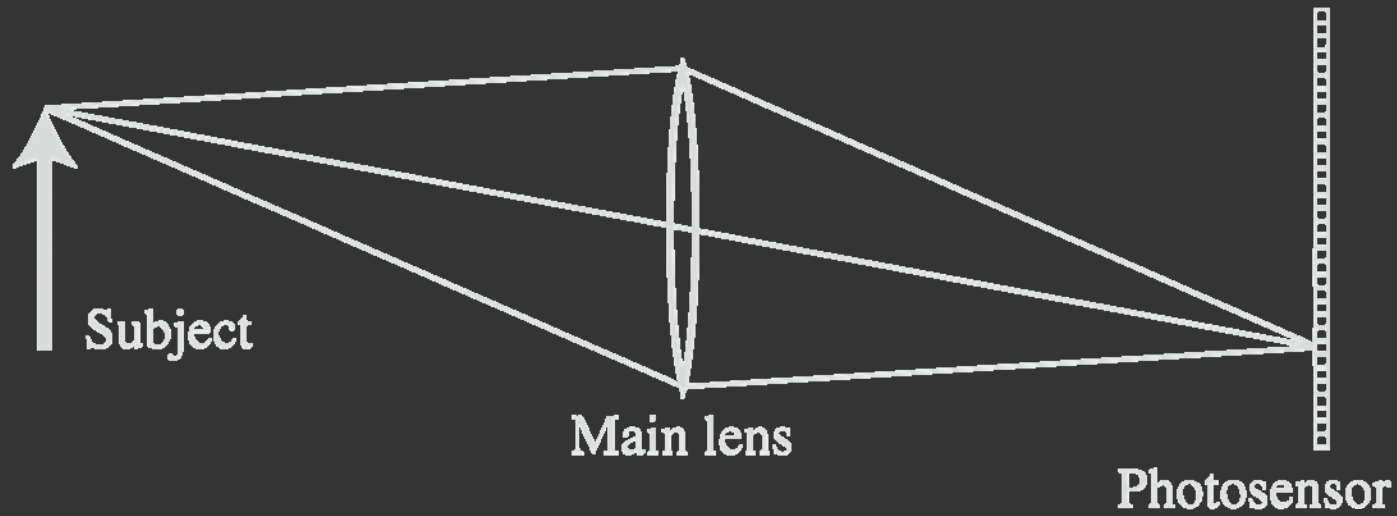


Encoded Blur Camera



Heterodyne Light Field Camera

# Lenslet-based Light Field camera



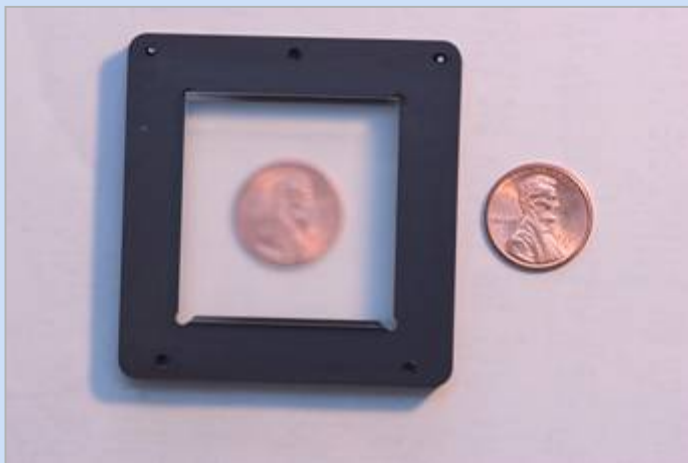
# Stanford Plenoptic Camera [Ng et al 2005]



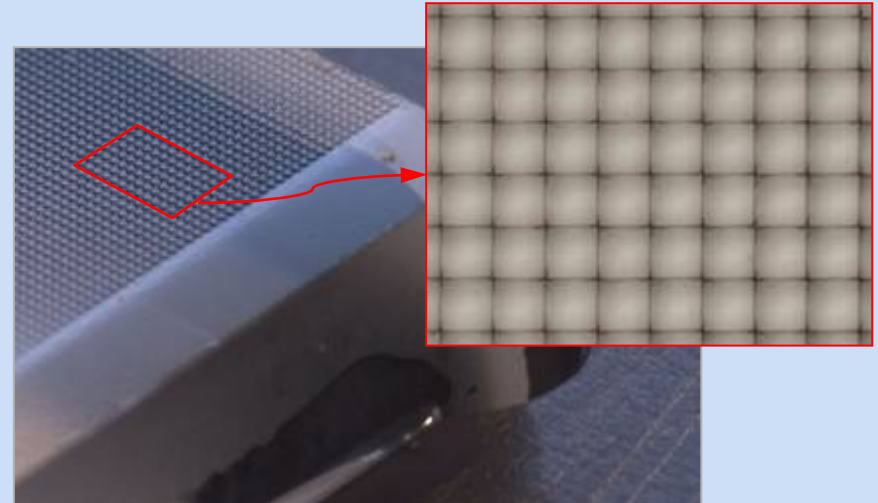
Contax medium format camera



Kodak 16-megapixel sensor

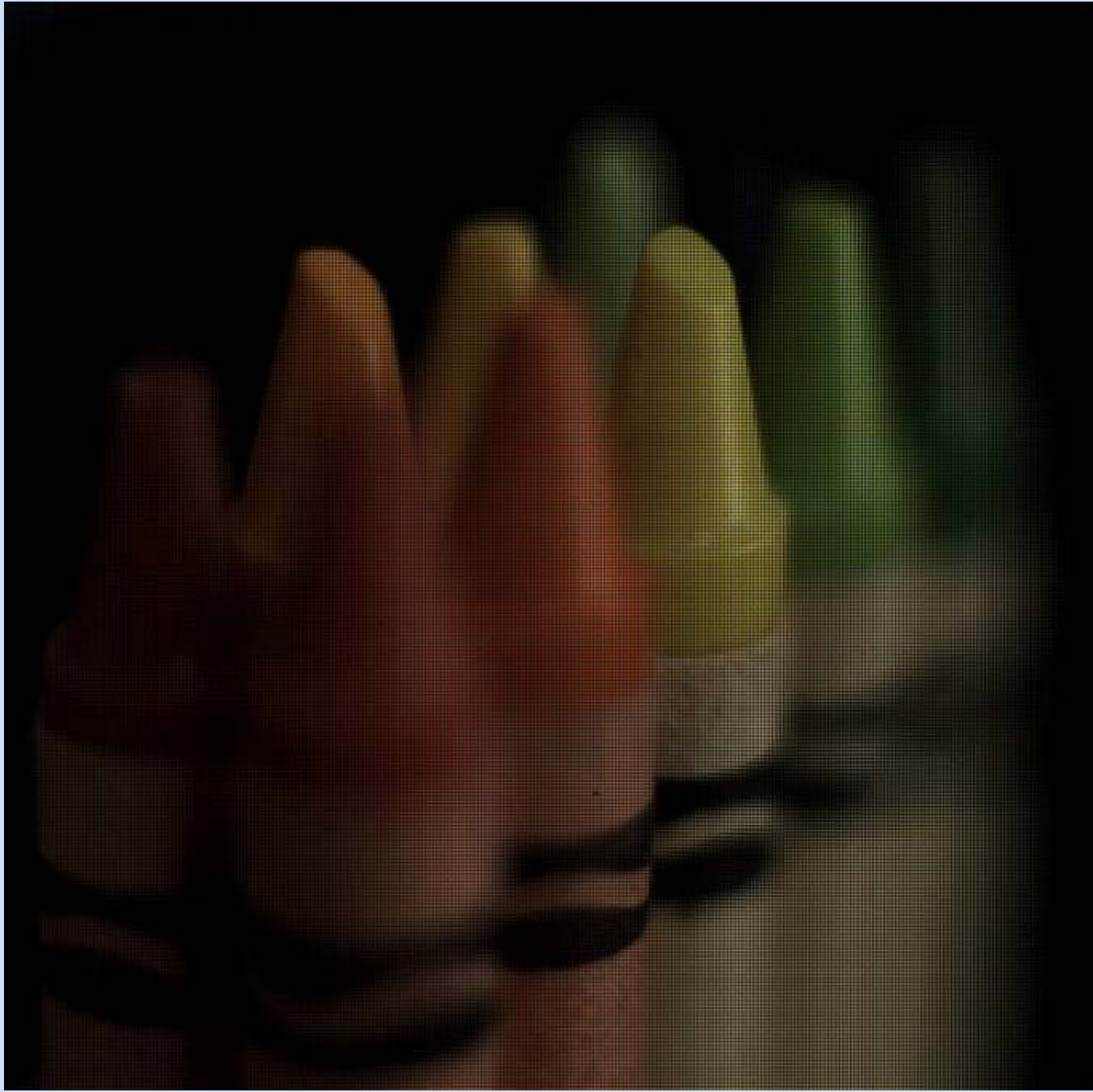


Adaptive Optics microlens array



125 $\mu$  square-sided microlenses

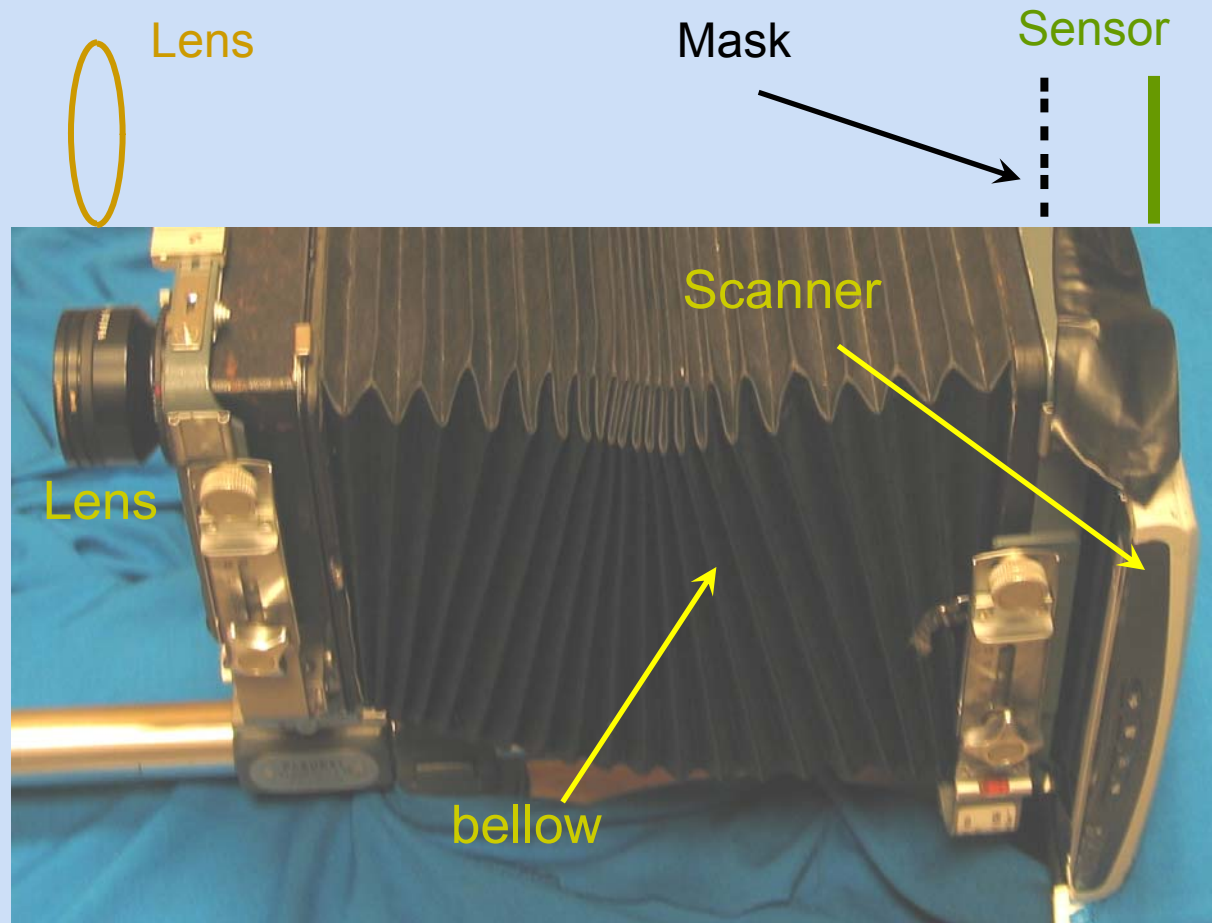
$$4000 \times 4000 \text{ pixels} \div 292 \times 292 \text{ lenses} = 14 \times 14 \text{ pixels per lens}$$



# Digital Refocusing (Lenslet array)

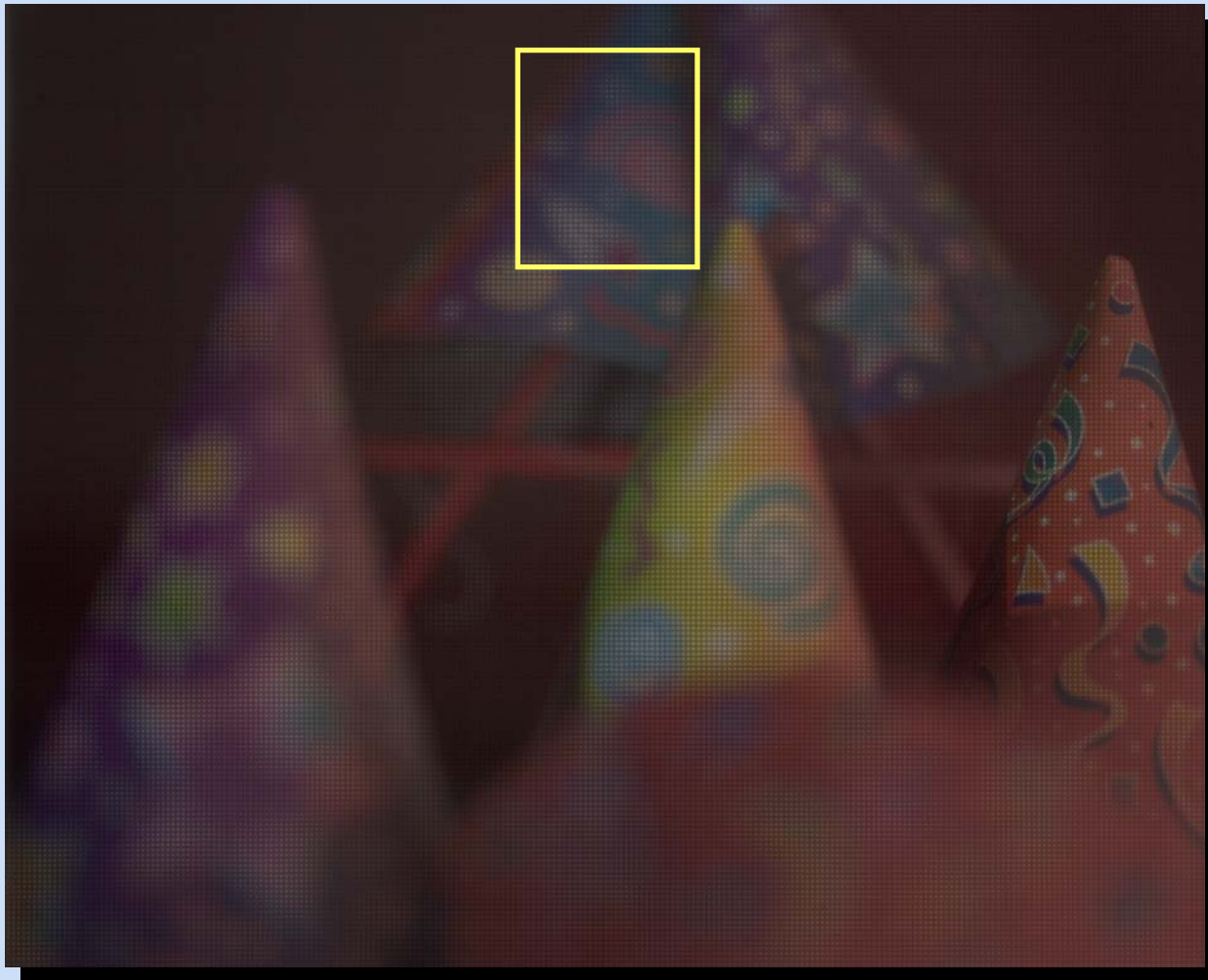


# Heterodyne Light Field Camera

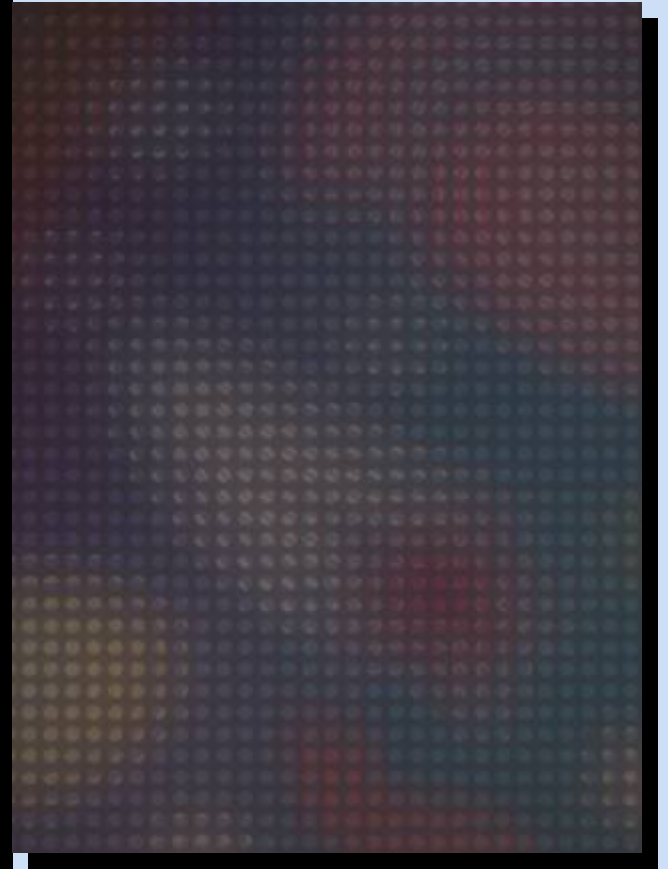


Canon flatbed scanner as the sensor.  
Mask is is  $\sim 1$  cm in front of the sensor.

# Capturing 4D light field

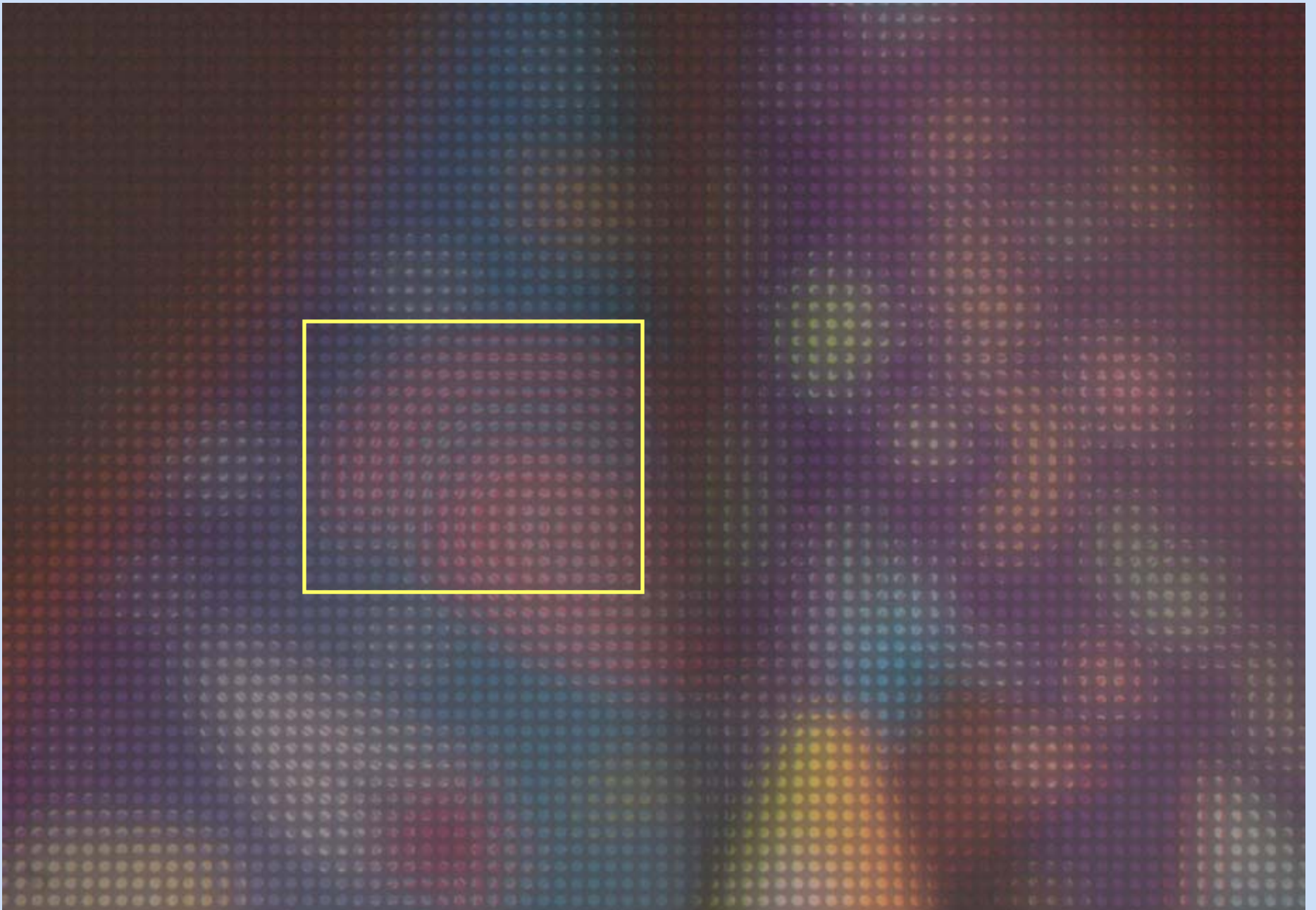


2D Sensor image



Zoom in showing  
light field encoding

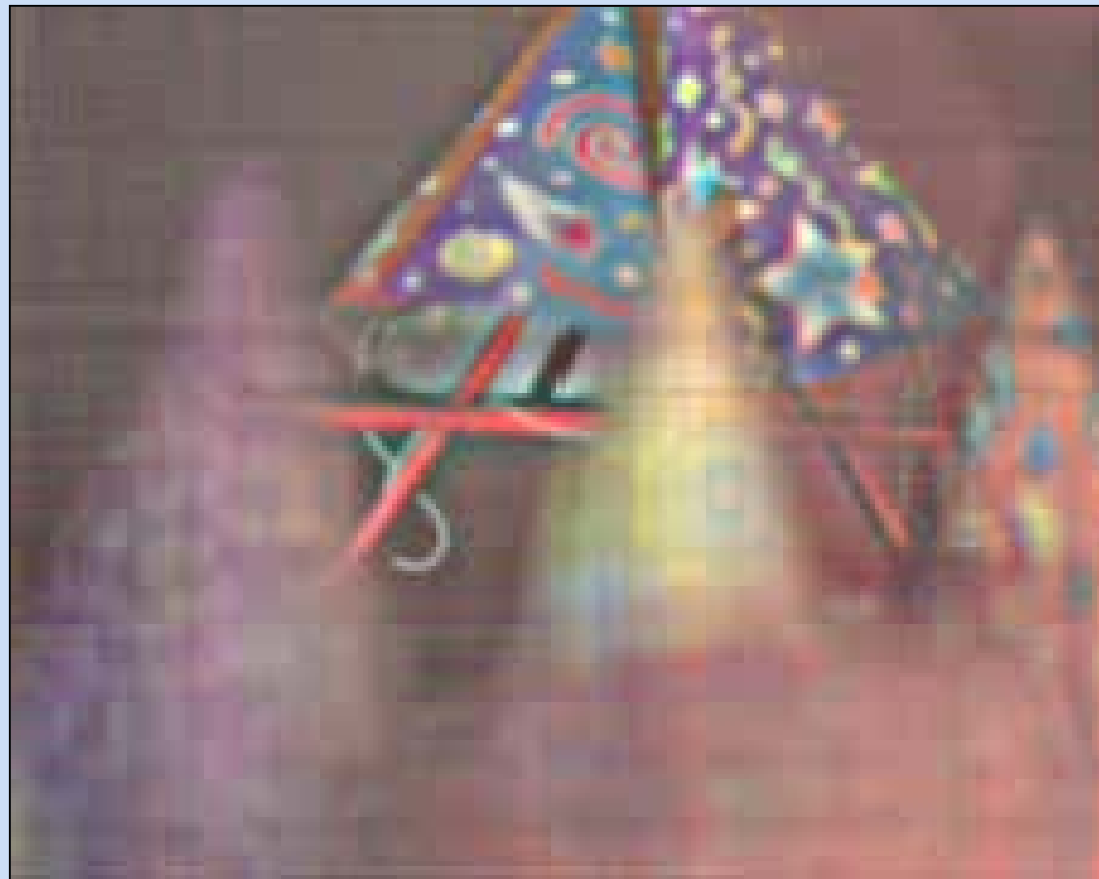






# Movie:

Digital Refocusing by taking  
2D Projections of 4D Light Field



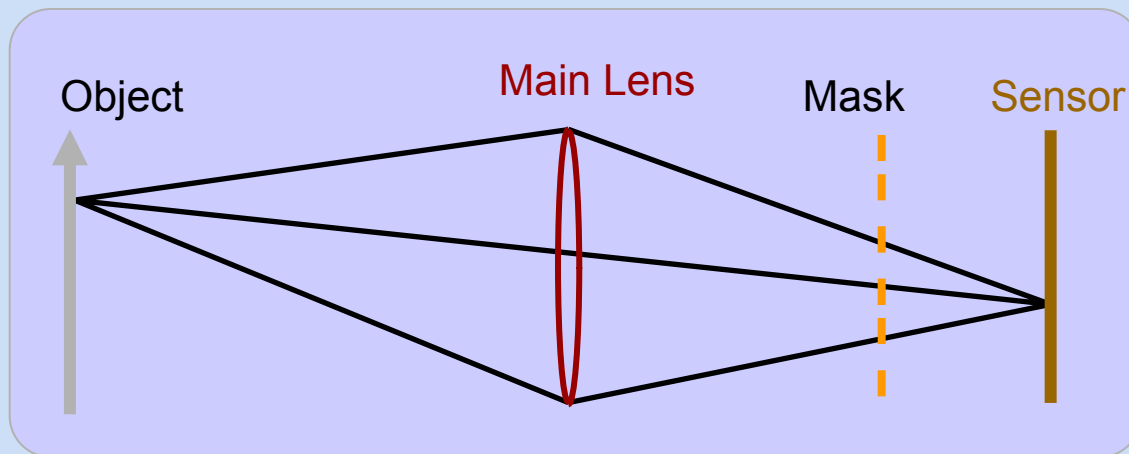
# Movie:

Different Views obtained from  
2D Slices of 4D light field



# How to Capture a 4D Signal with a 2D Sensor ?

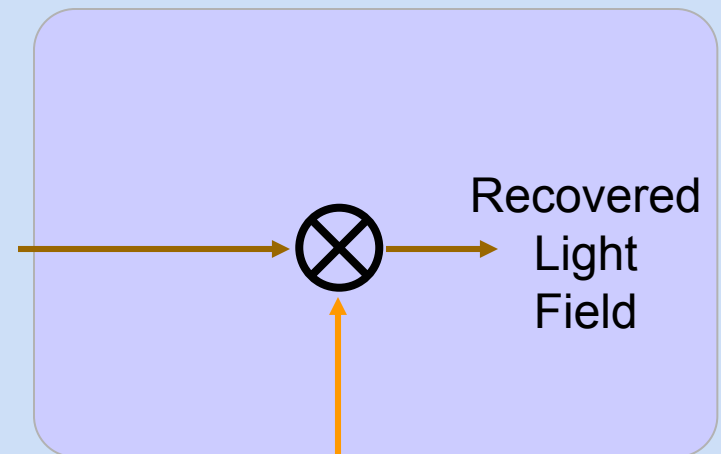
## Mask-based Modulation



Photographic  
Signal  
(Light Field) →

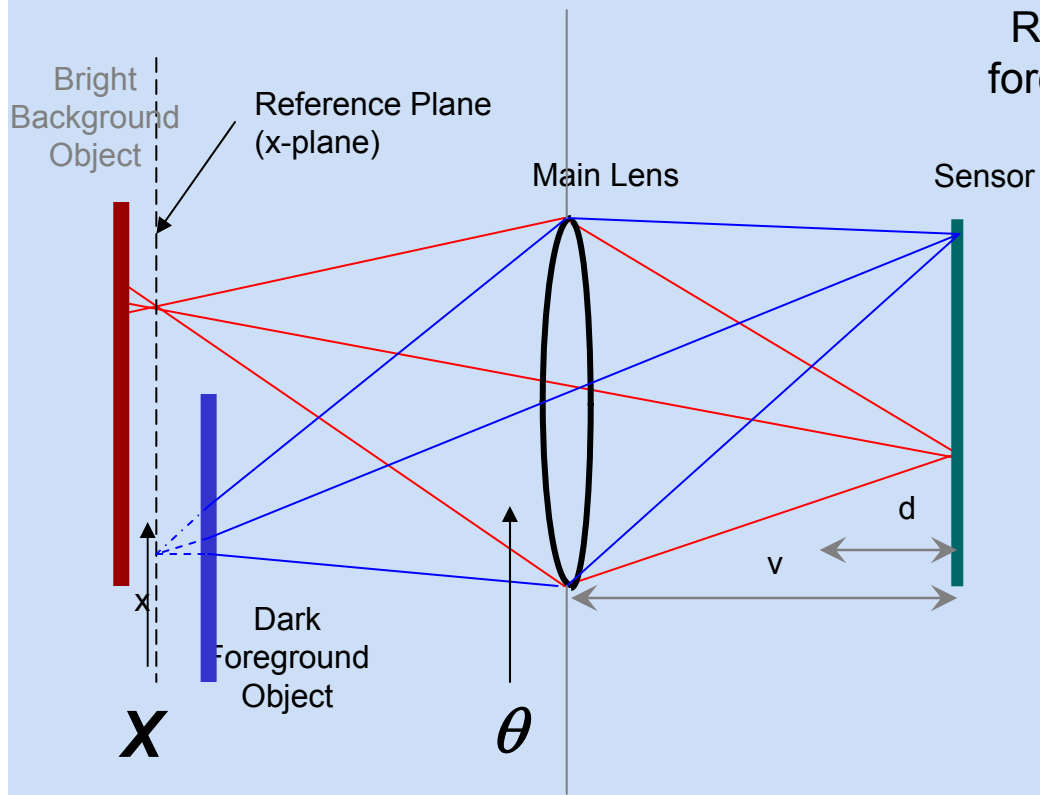
Carrier  
(High  
Frequency)  
Incident  
Modulated  
Signal

## Software Demodulation



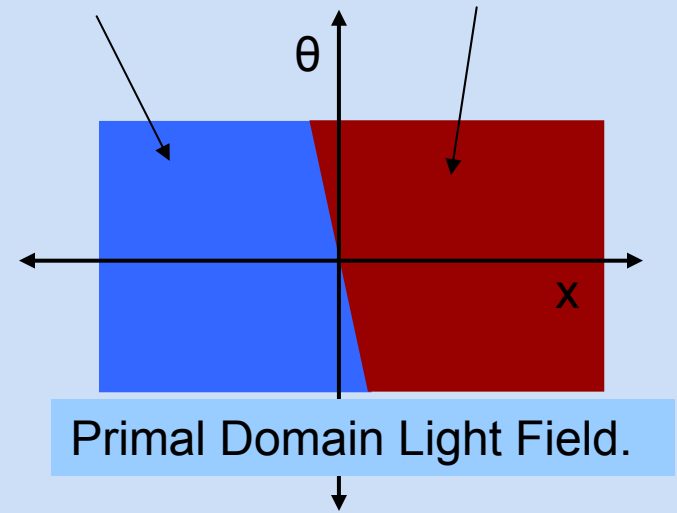
Reference  
Carrier

Recovered  
Light  
Field

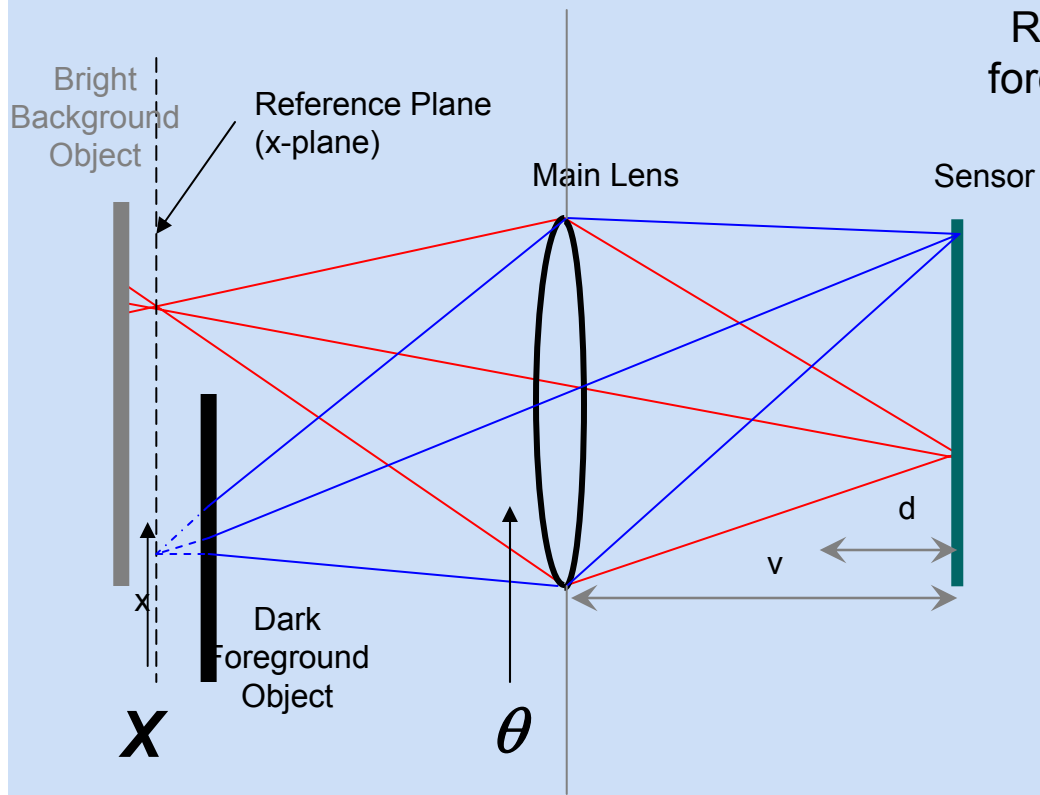


Rays from Dark foreground Object

Rays from Bright Background Object

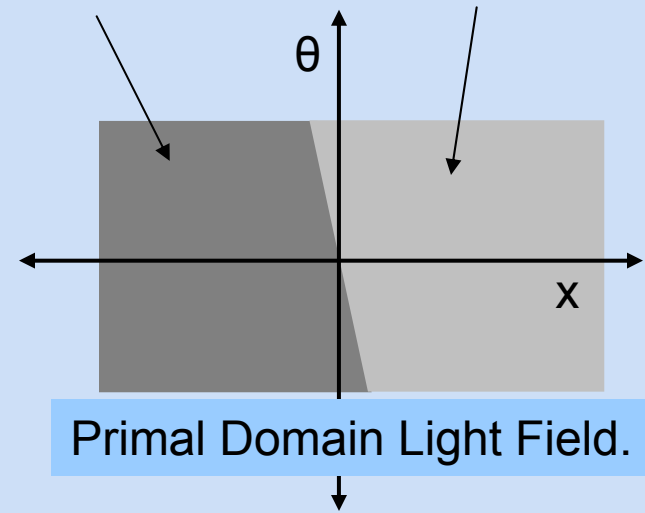


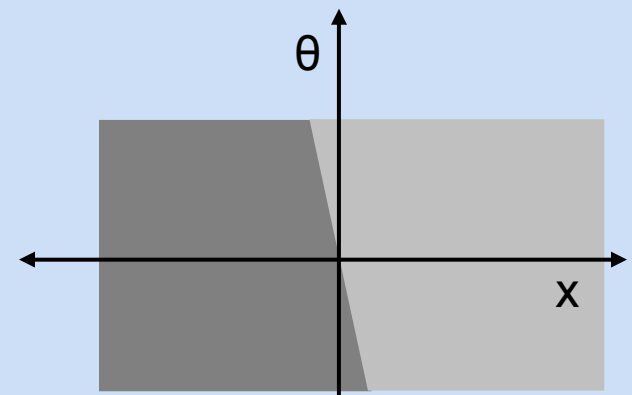
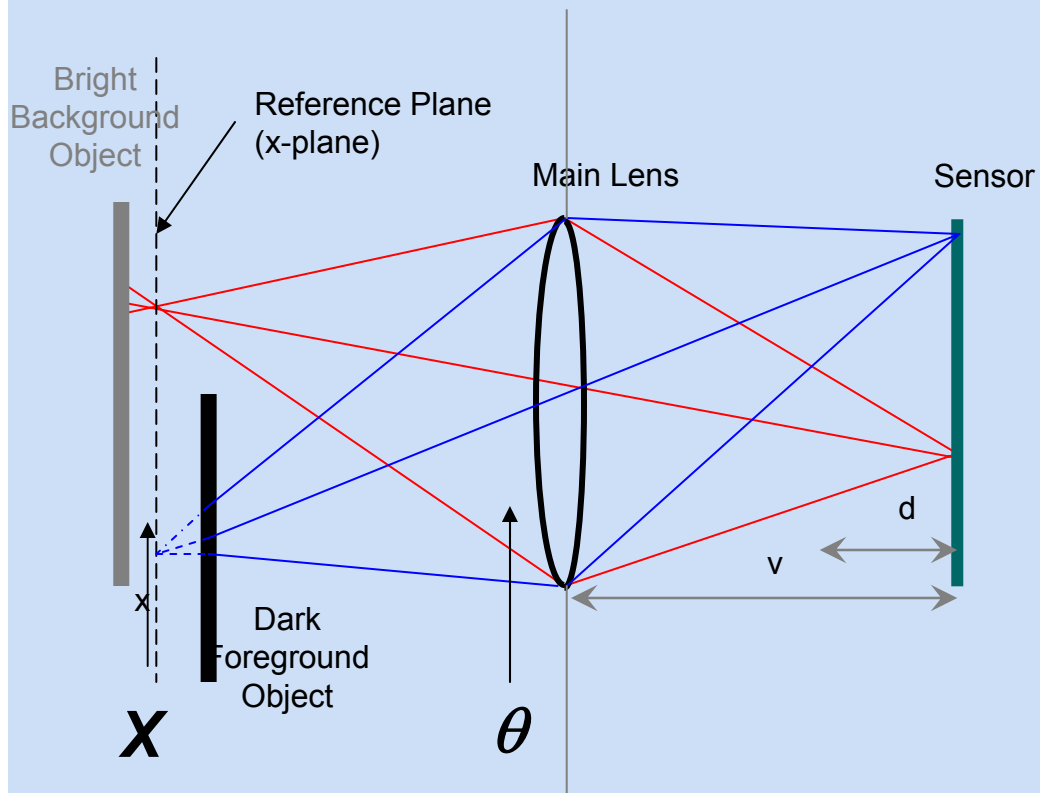
Primal Domain Light Field.



Rays from Dark foreground Object

Rays from Bright Background Object

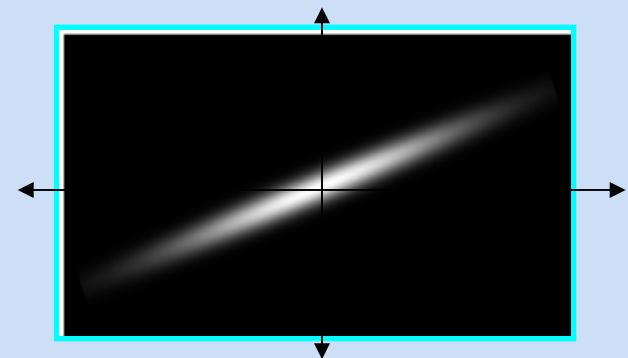




Primal Domain Light Field.

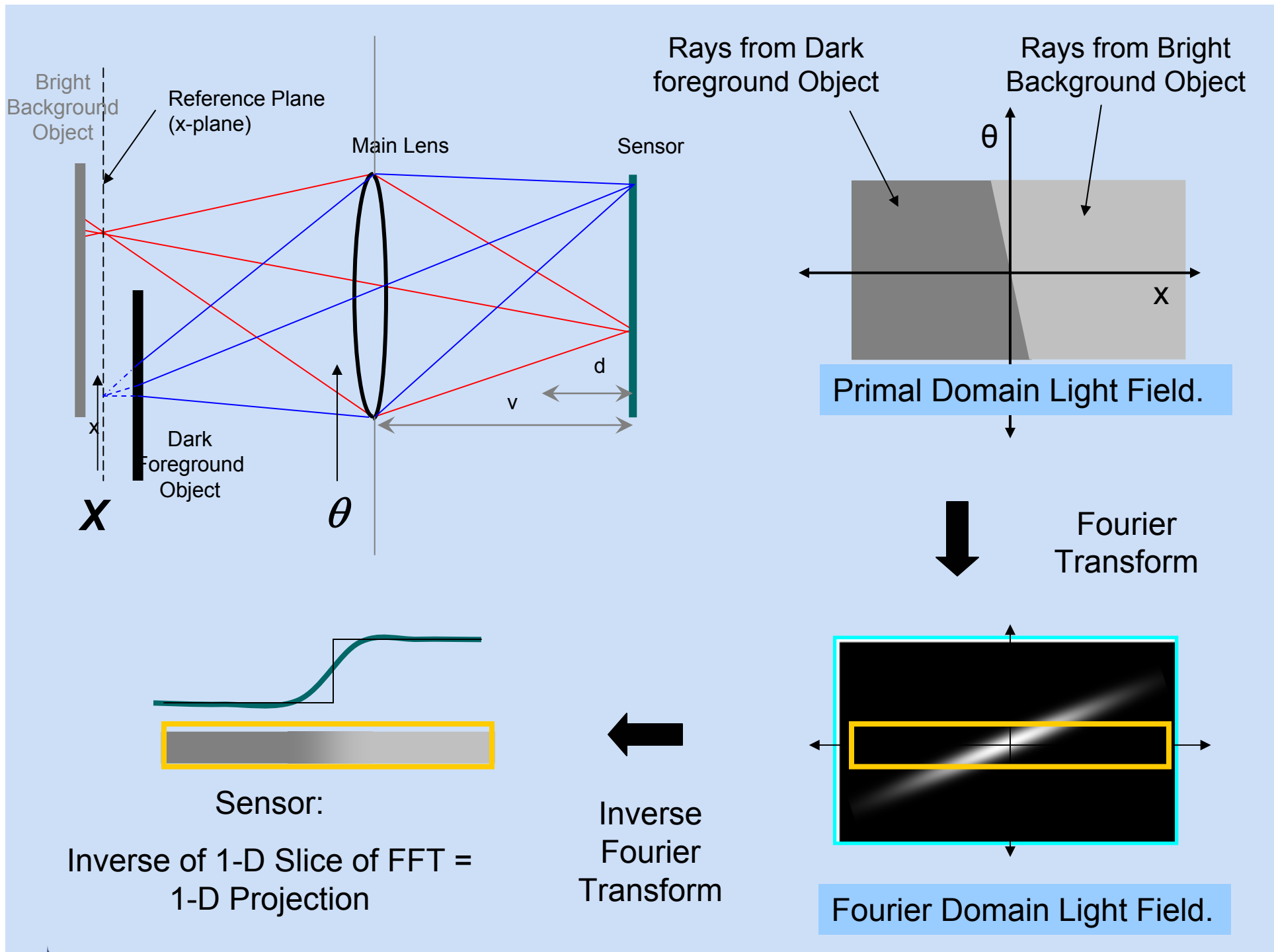


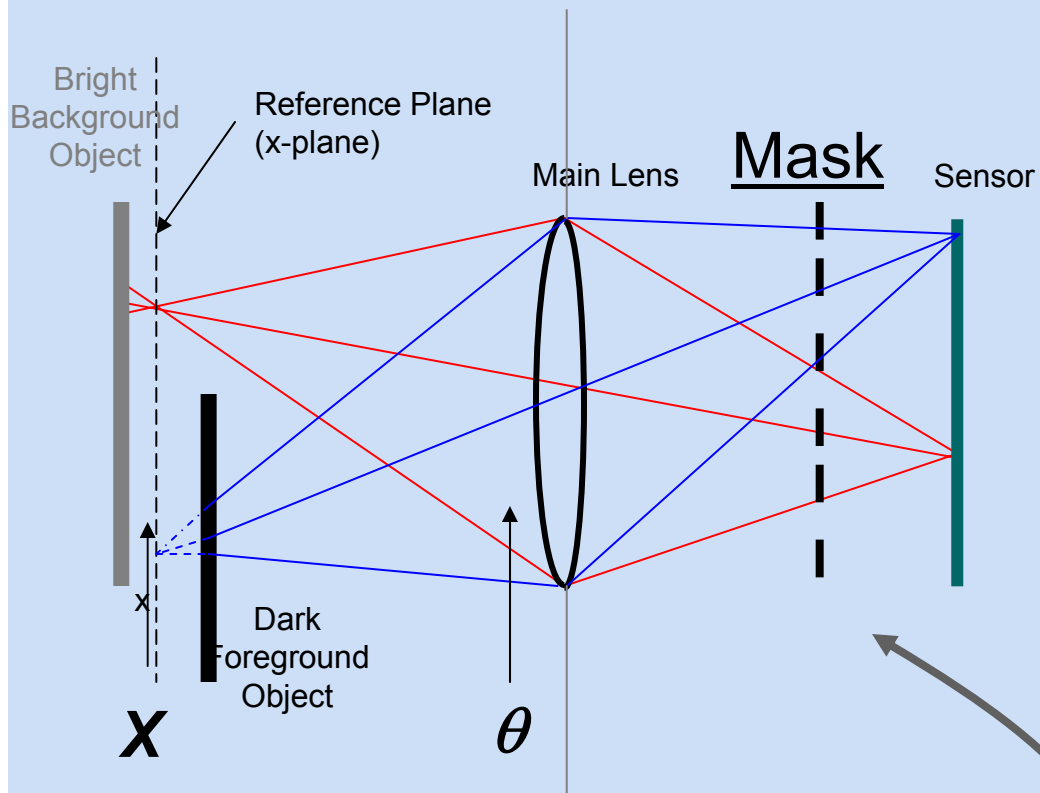
Fourier Transform



Fourier Domain Light Field.



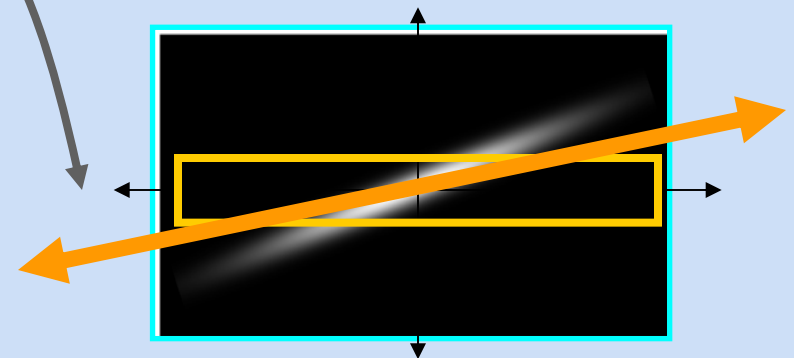




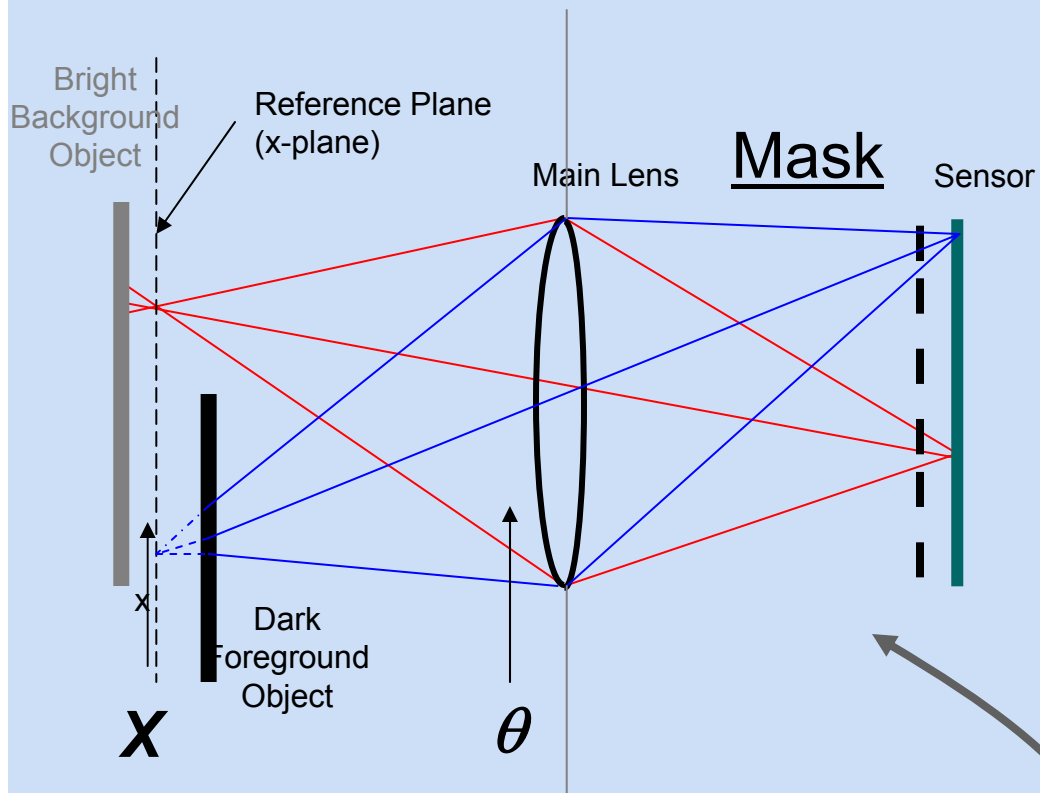
**Incident Light Field =  
Multiplication with the  
Light Field of the  
mask**

Fourier  
Transform

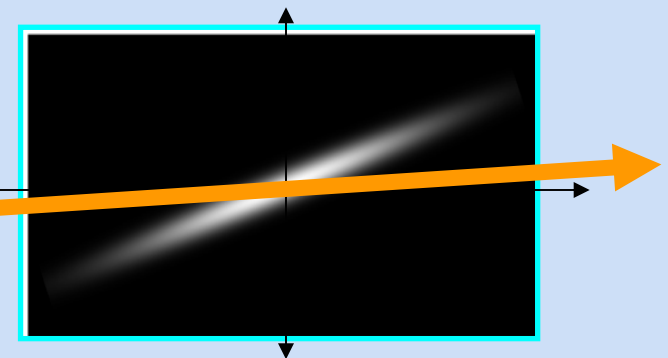
**Convolution with  
the Fourier  
transform of the  
Mask**



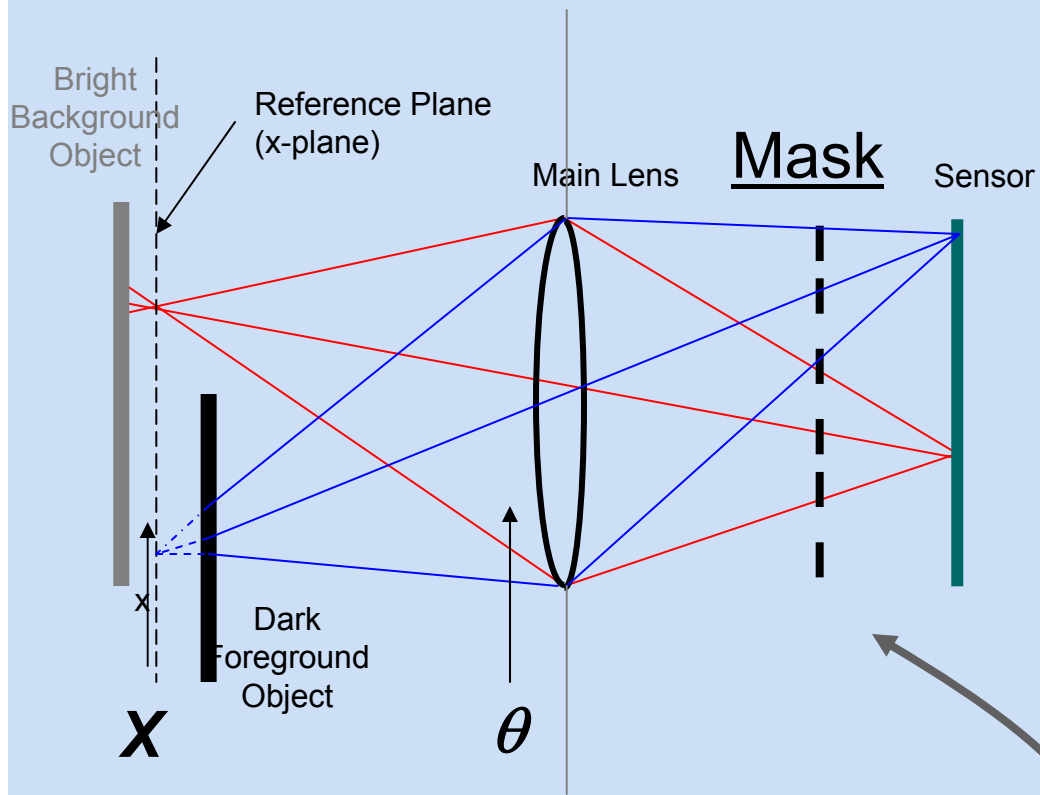
Fourier Domain Light Field.



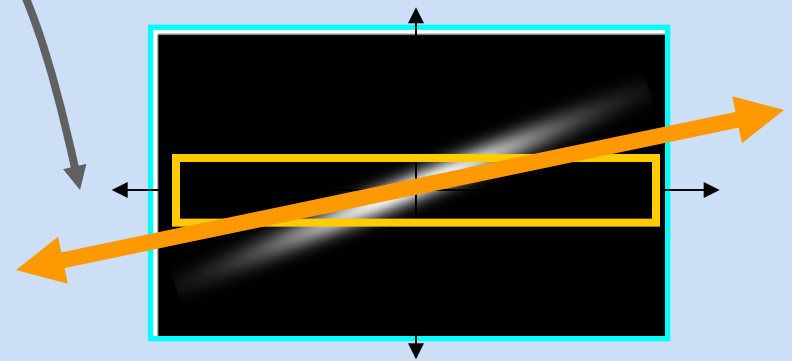
**Convolution with  
the Fourier  
transform of the  
mask**



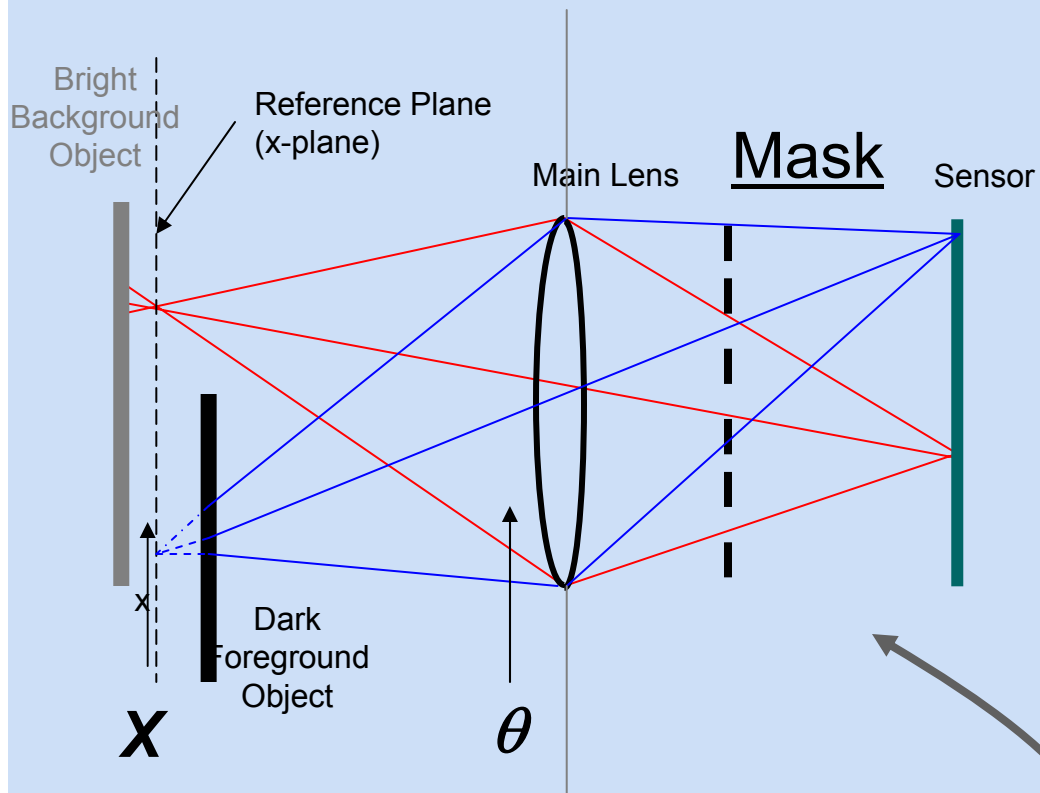
**Fourier Domain Light Field.**



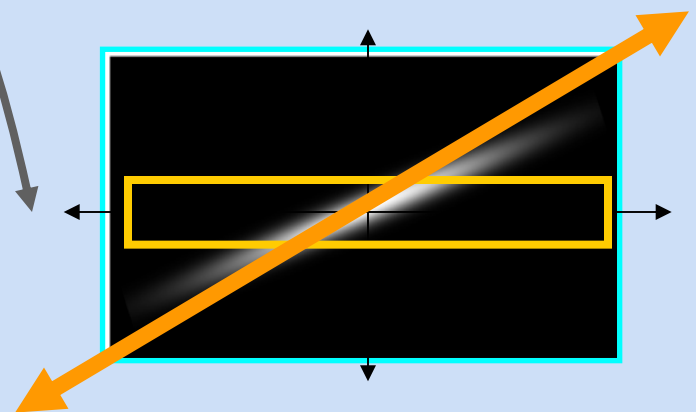
Convolution with  
the Fourier  
transform of the  
mask



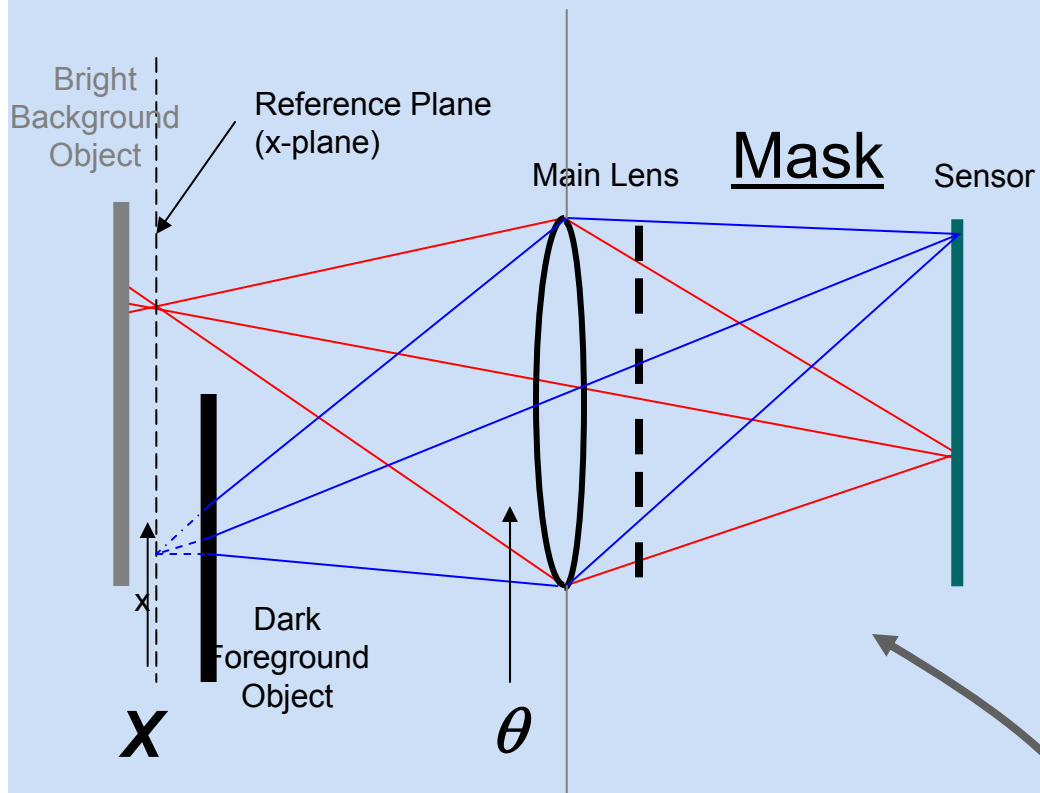
Fourier Domain Light Field.



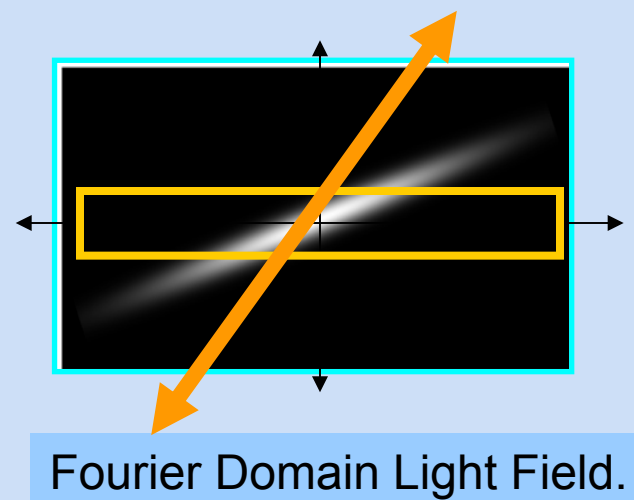
Convolution with  
the Fourier  
transform of the  
mask

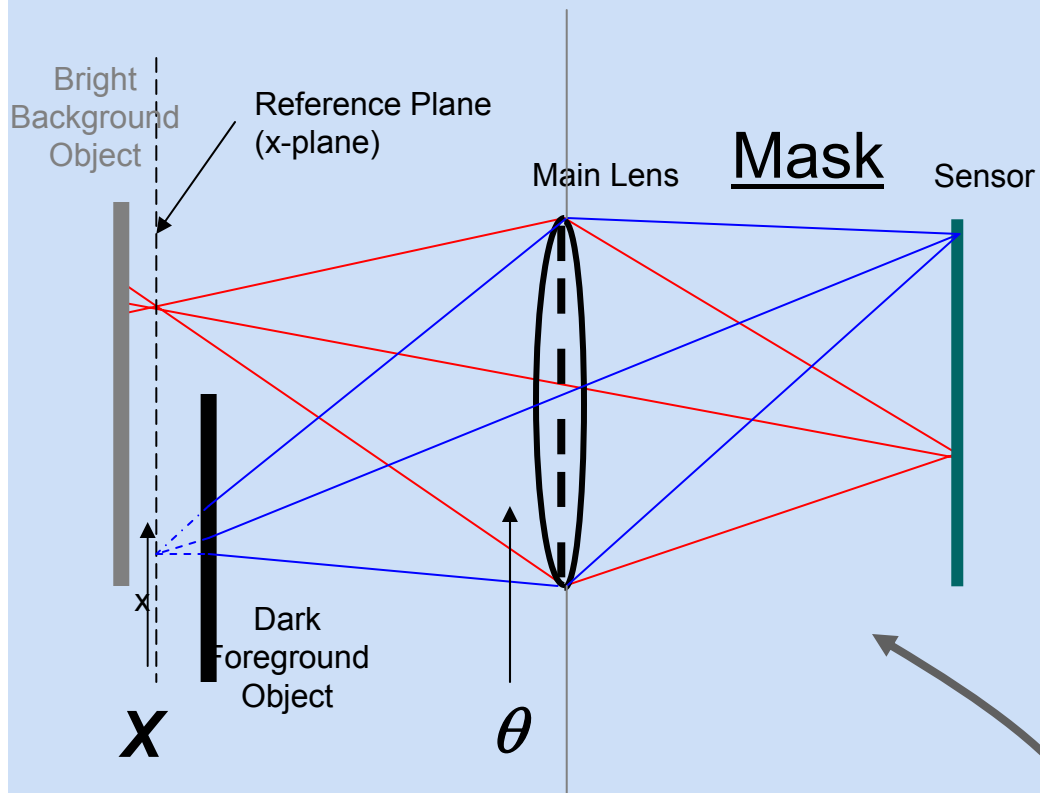


Fourier Domain Light Field.

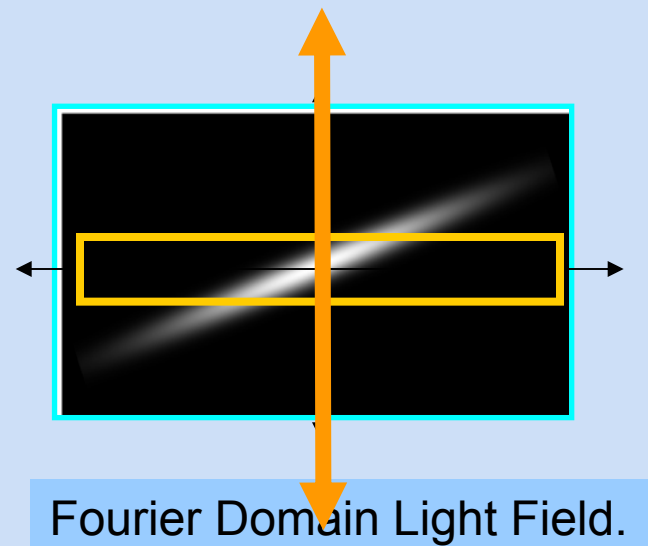


Convolution with  
the Fourier  
transform of the  
mask

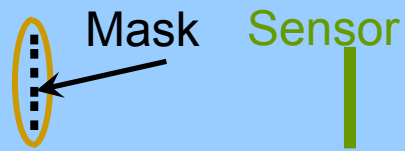
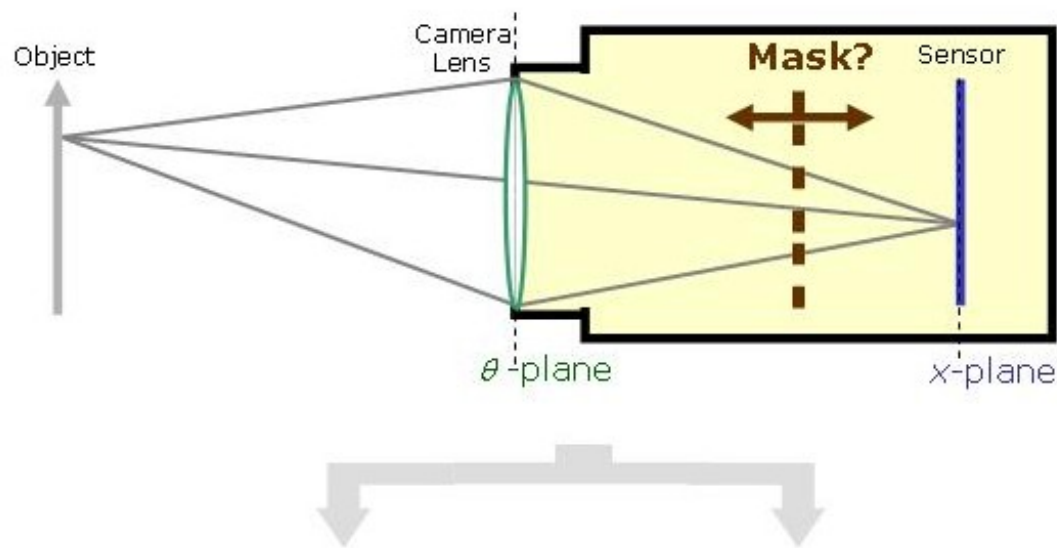




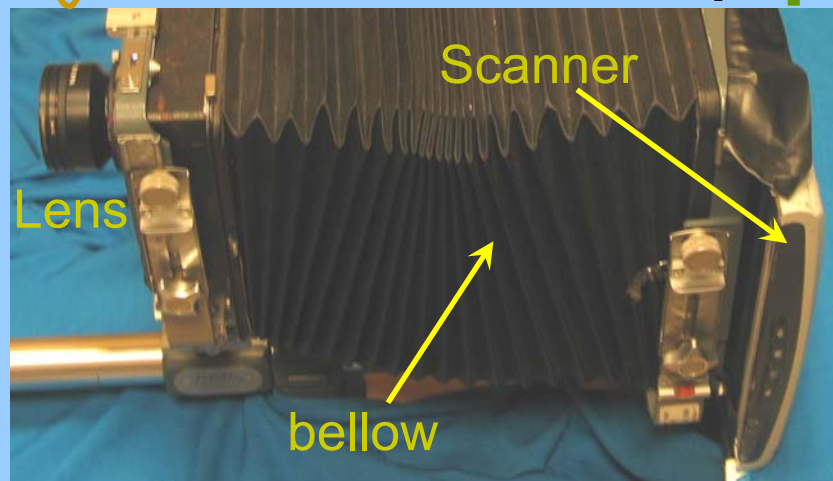
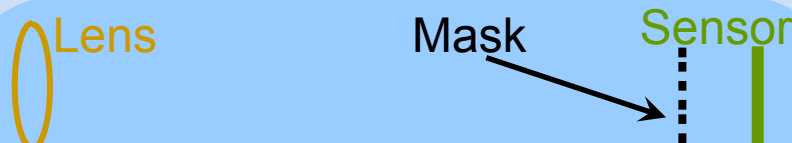
**Convolution with  
the Fourier  
transform of the  
mask**



# Coding Light Field Entering a Camera via a Mask



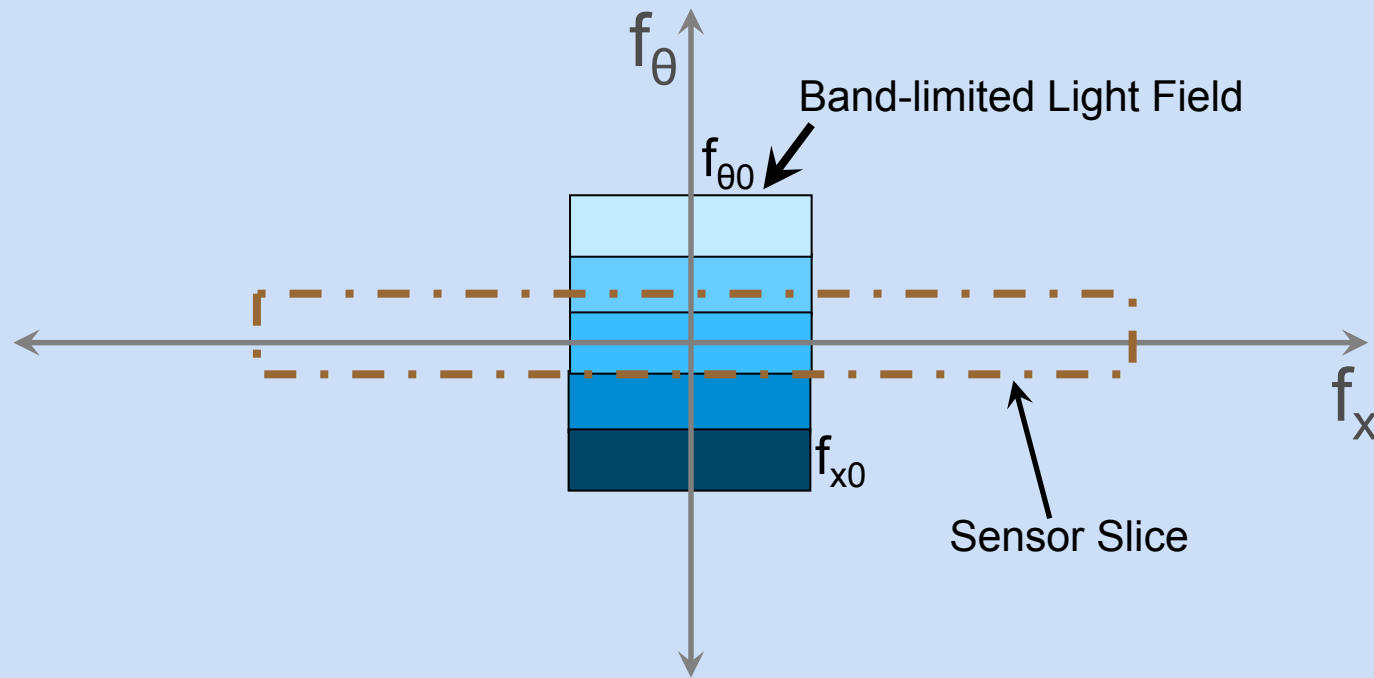
Encoded Blur Camera



Heterodyne Light Field Camera

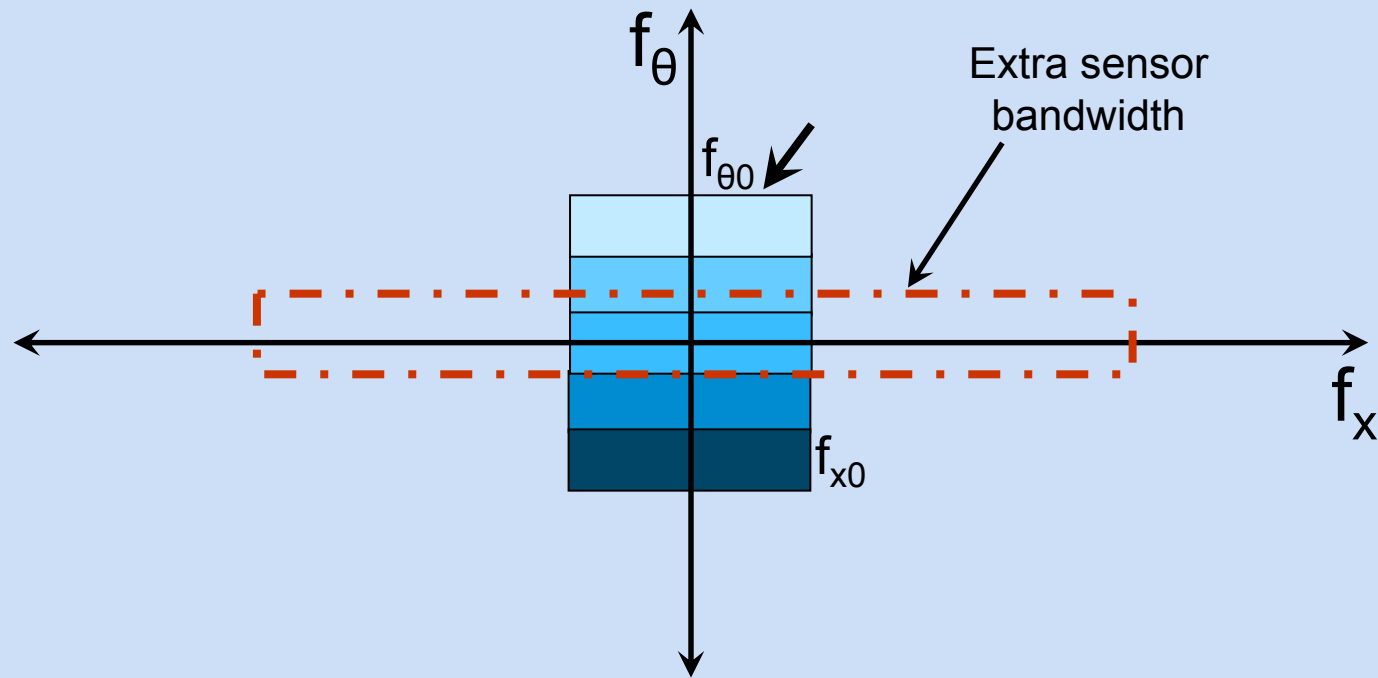


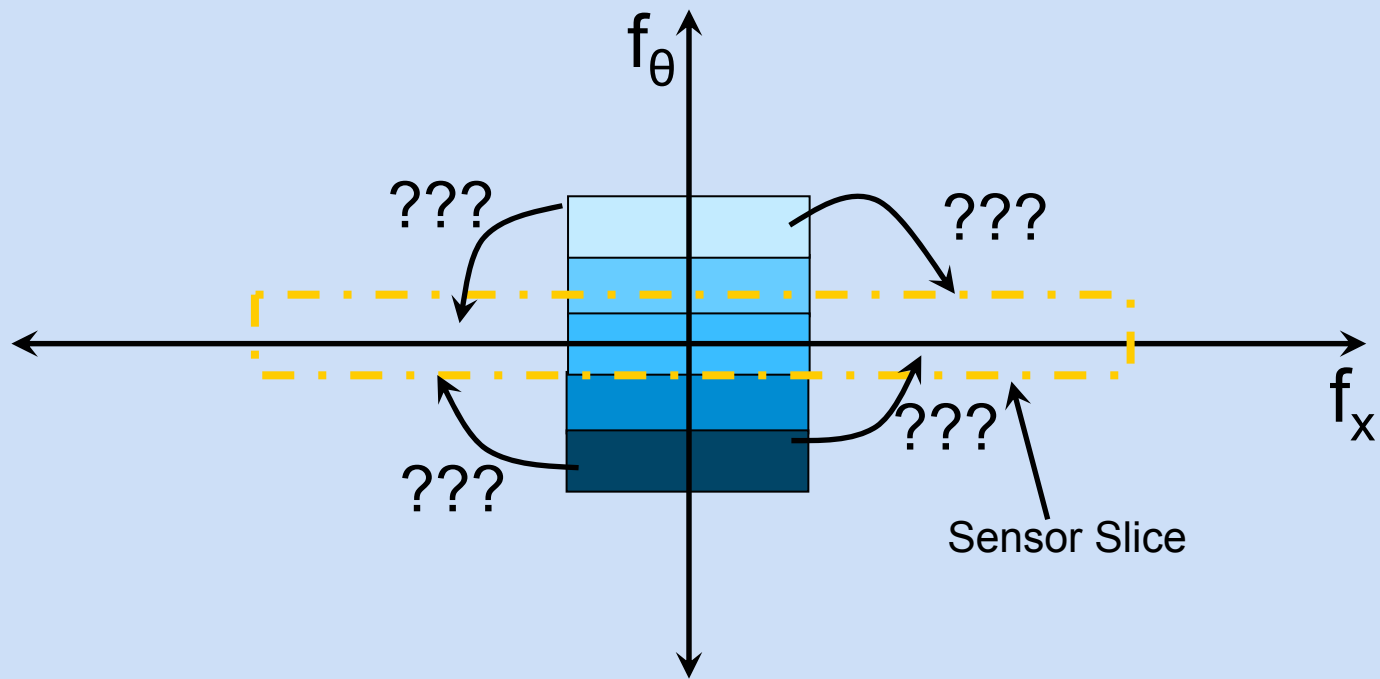
# How to Capture 4D Light Field with 2D Sensor ?



Fourier Light Field Space

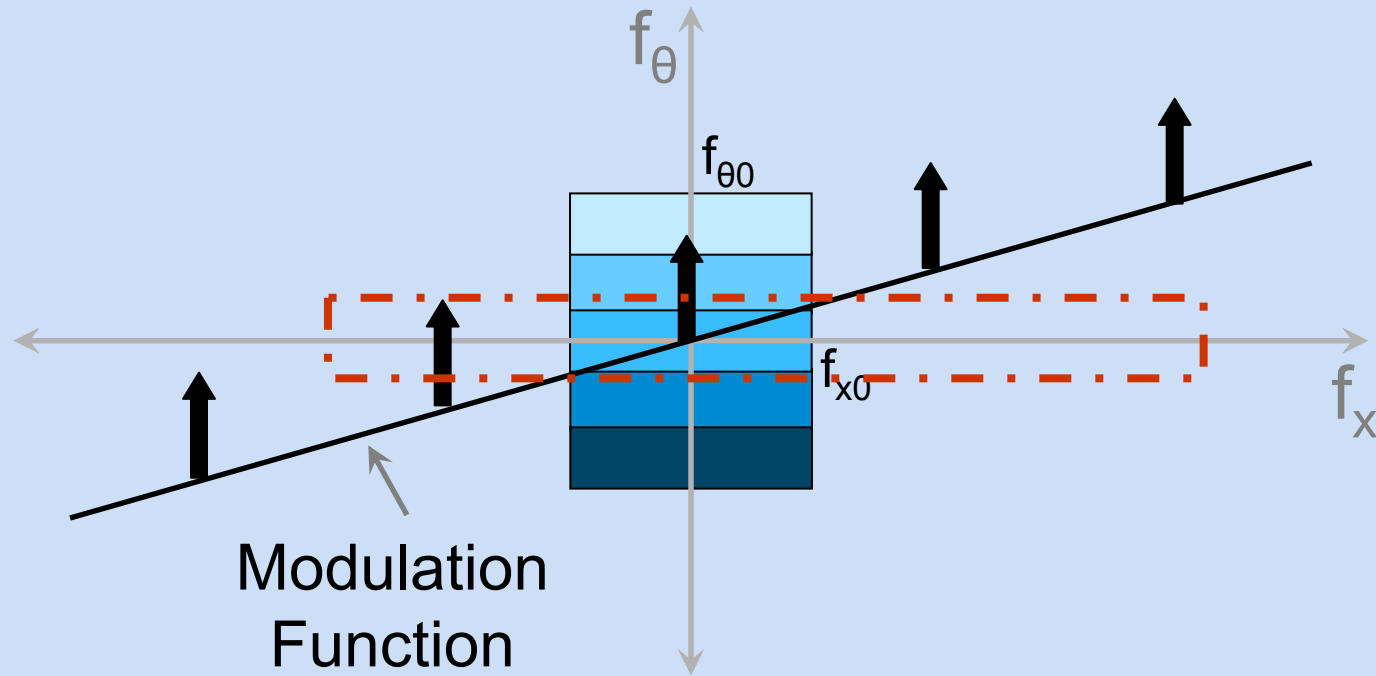
Extra sensor bandwidth cannot capture  
extra *dimension* of the light field





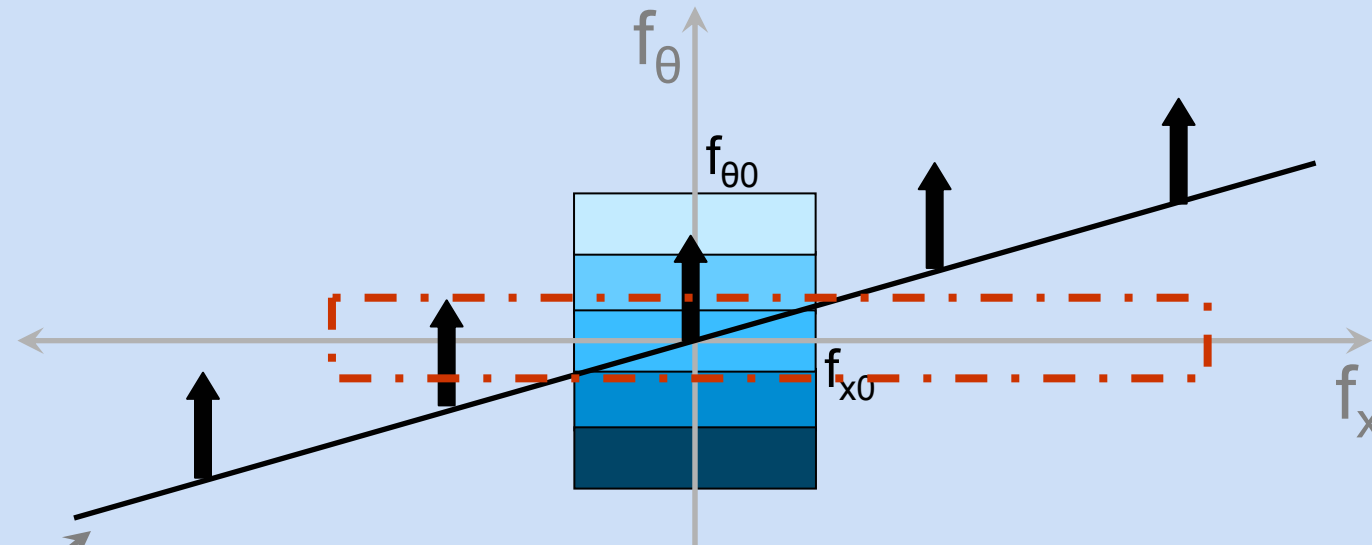
# Solution: Modulation Theorem

Make spectral copies of 2D light field

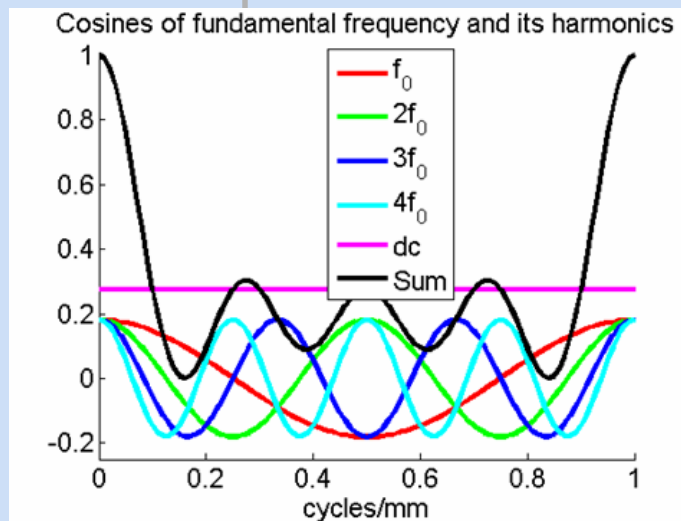


# Solution: Modulation Theorem

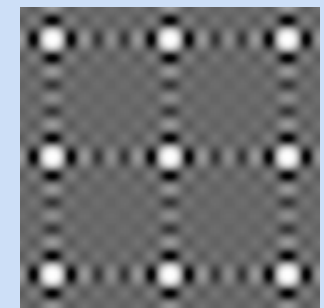
Make spectral copies of 2D light field



Modulation Function  
= Sum of Cosines



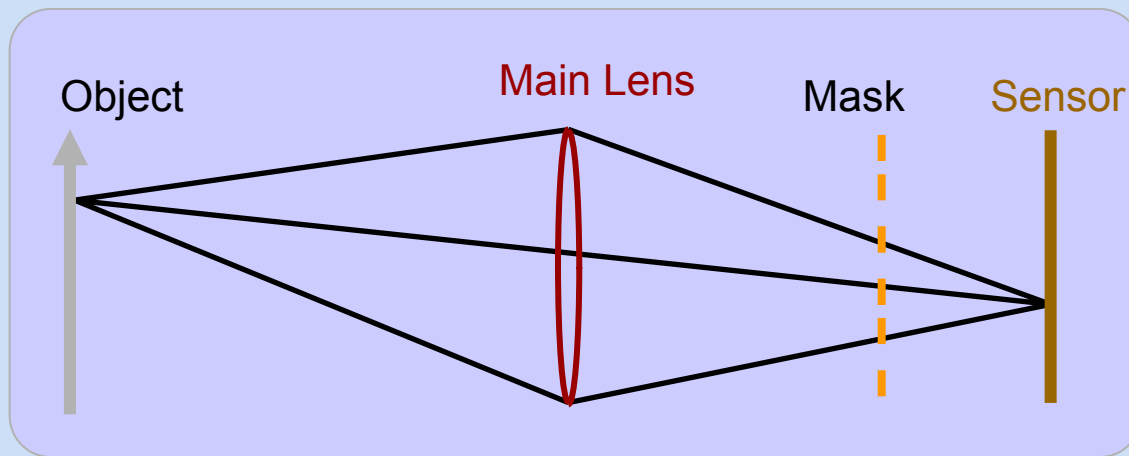
Mask Tile



$1/f_0$

# How to Capture a 4D Signal with a 2D Sensor ?

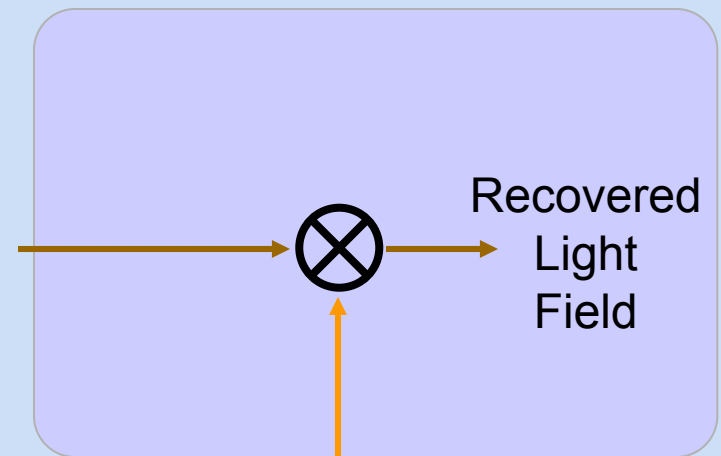
## Mask-based Modulation



Photographic  
Signal  
(Light Field) →

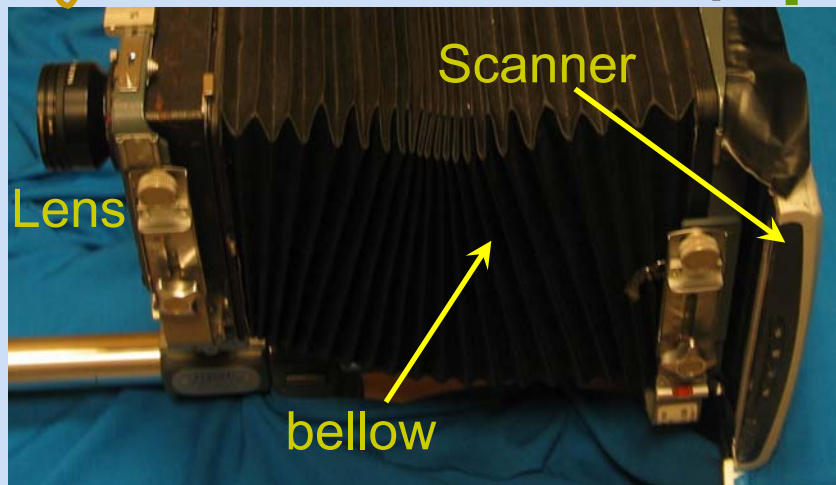
Carrier  
(High  
Frequency)  
Incident  
Modulated  
Signal

## Software Demodulation

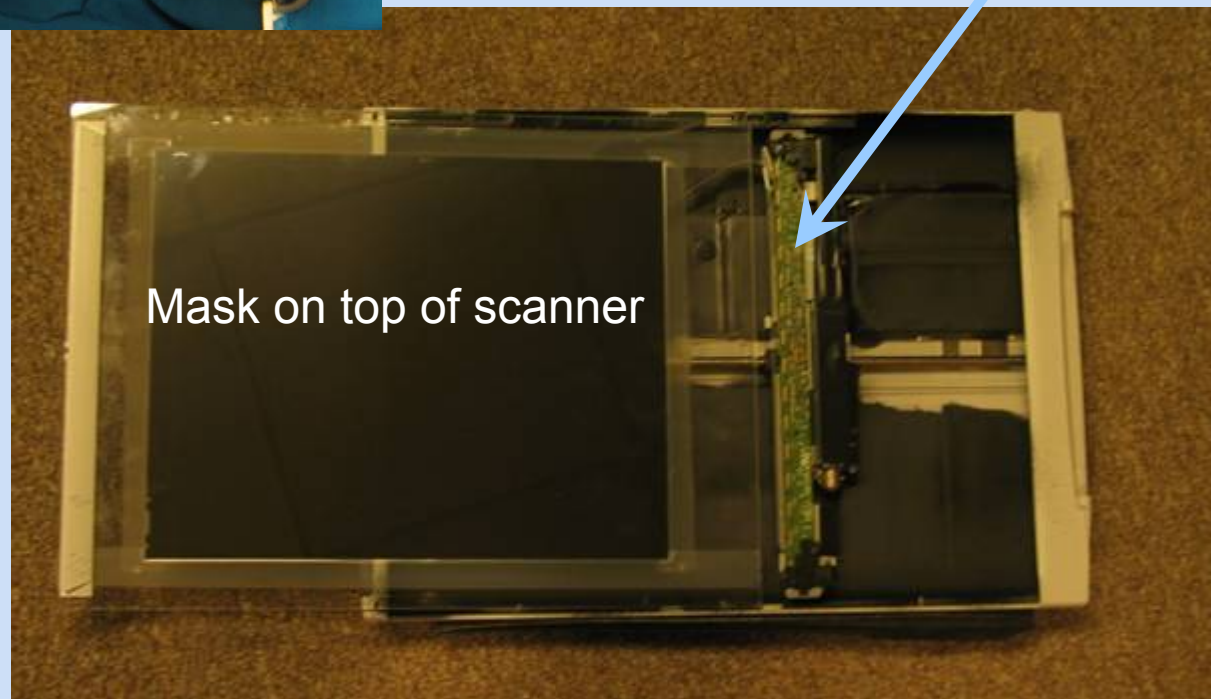


Reference  
Carrier

Recovered  
Light  
Field

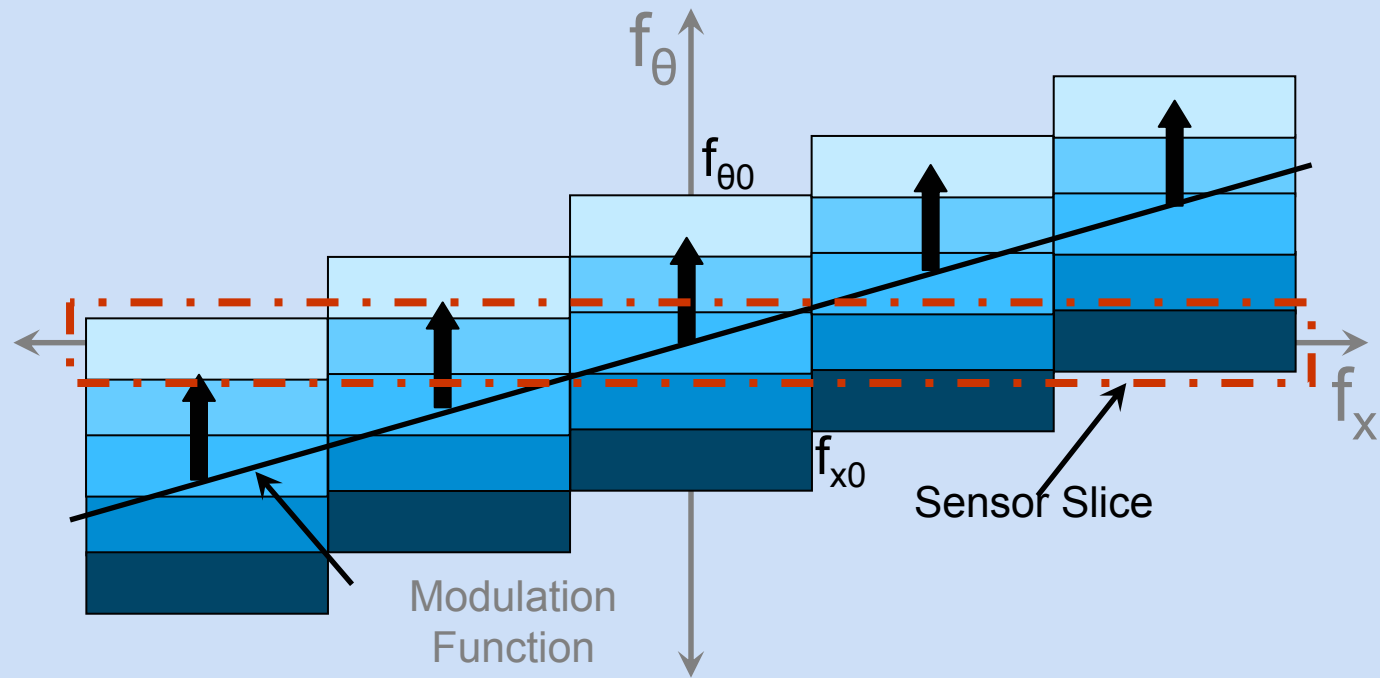


Scanner 1D sensor



Mask = 4 cosines = 9 impulses in Fourier transform  
= 9 angular samples

# Sensor slice captures entire Light Field



## Modulated Light Field



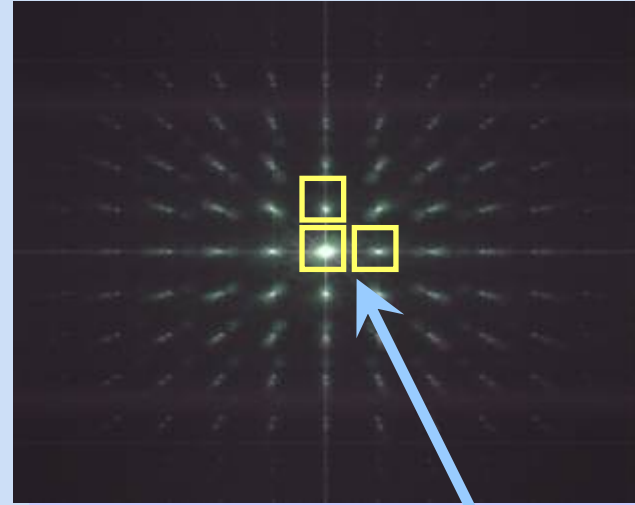
# Computing 4D Light Field

2D Sensor image,  $1629 \times 2052$



2D  
FFT

2D Fourier Transform,  $1629 \times 2052$



$9 \times 9 = 81$  such  
tiles

Reshape 2D tiles into 4D planes

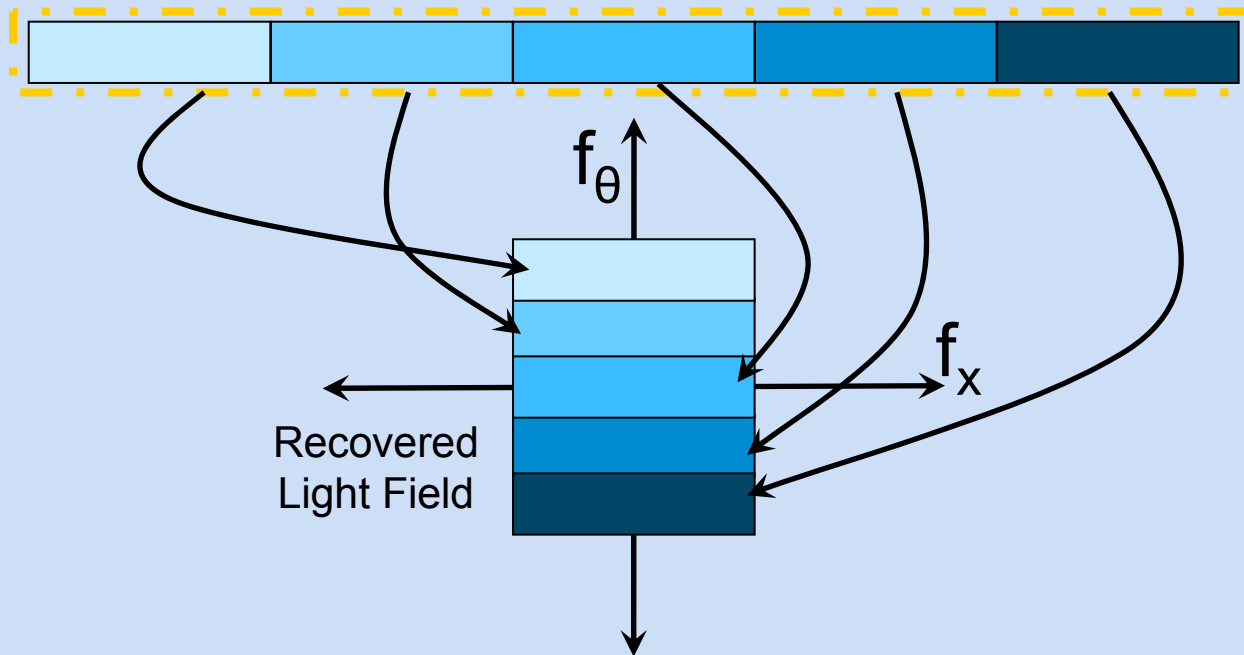
$181 \times 228 \times 9 \times 9$



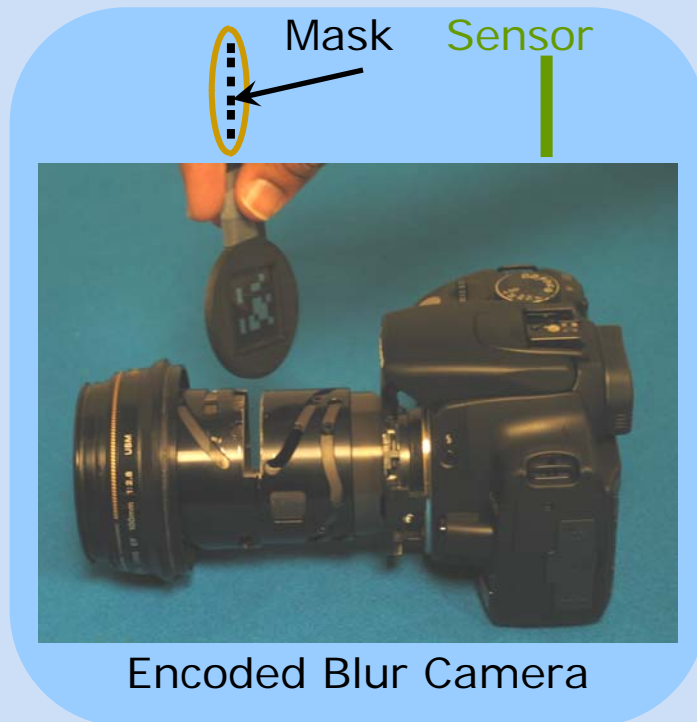
4D Light Field  
 $181 \times 228 \times 9 \times 9$

4D  
IFFT

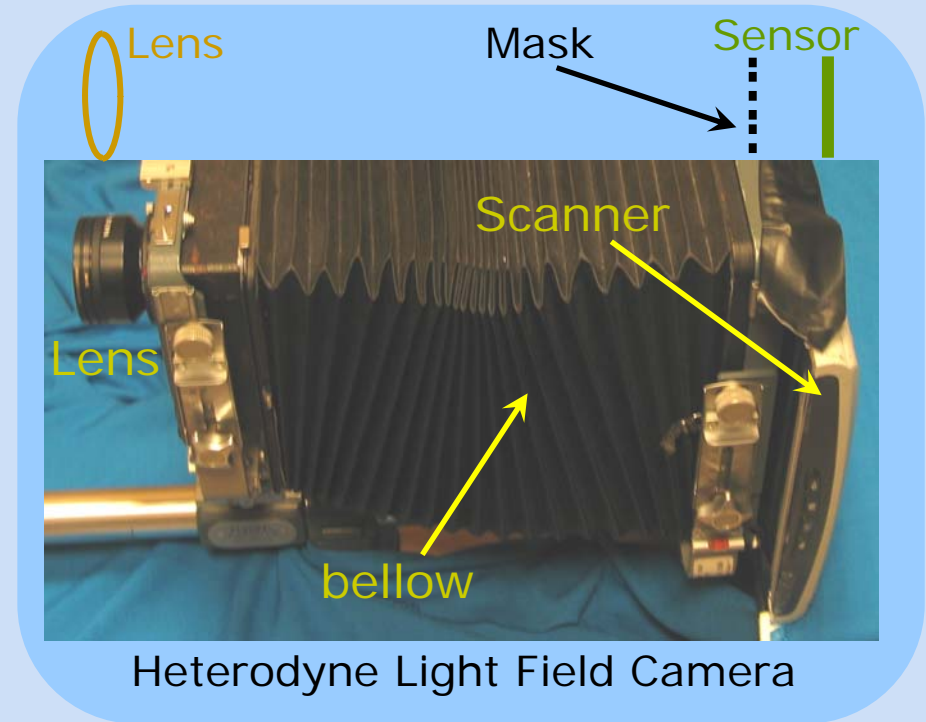
To recover light field from sensor slice,  
*Reshape* in Fourier tiles



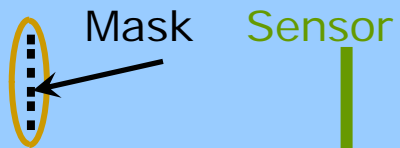
# Coded Masks For Cameras



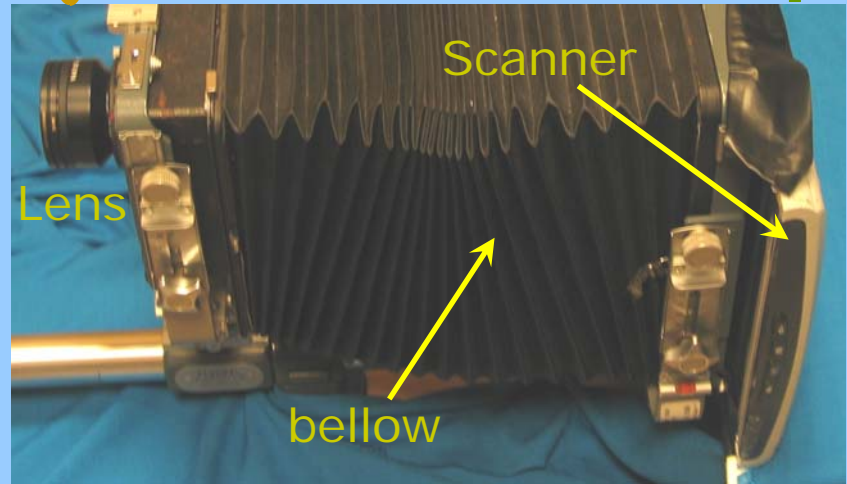
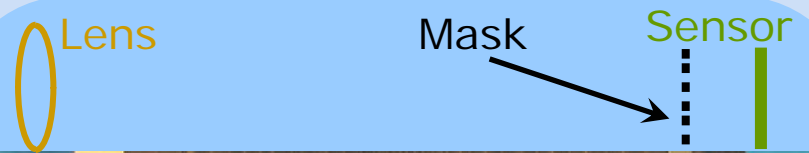
- Capture Coded Blur
- Full resolution digital refocussing
- Coarse, **broadband** mask in aperture
- Convolution of sharp image with mask



- Capture Light Field
- Complex refocussing at reduced resolution
- Fine, **narrowband** mask close to sensor
- Modulation of incoming light field by mask



Encoded Blur Camera



Heterodyne Light Field Camera



Fourier transform of optimal 1D mask pattern is a set of 1D impulses



Optimal 1D Mask is sum of cosines

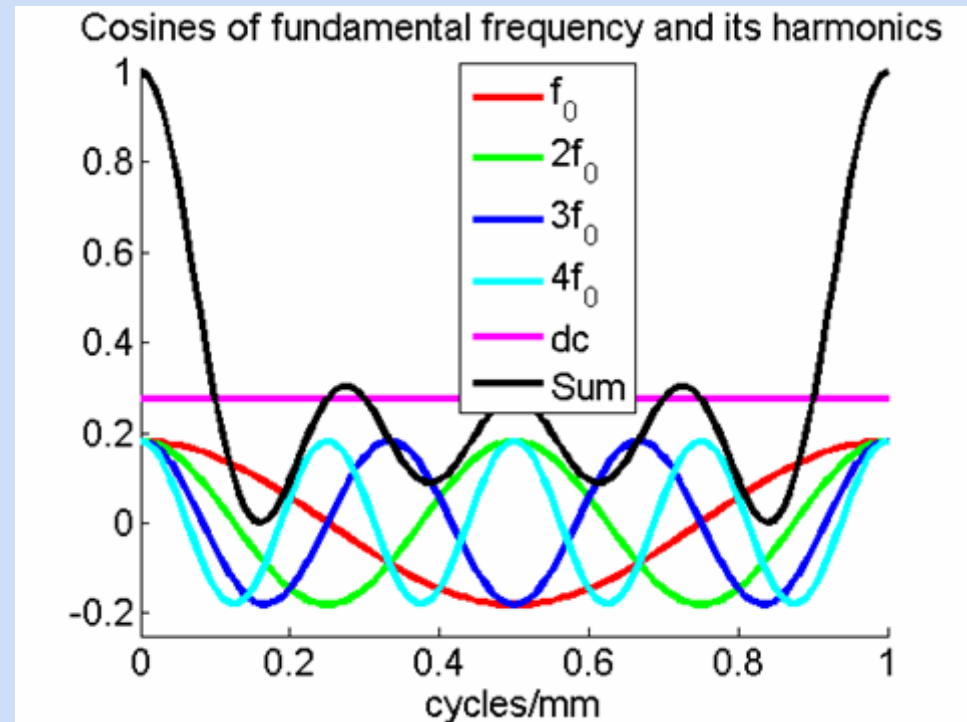
Optimal 2D mask: Sum of cosines in 2D

Number of angular samples = Number of impulses  
in Fourier transform of the mask along that  
dimension



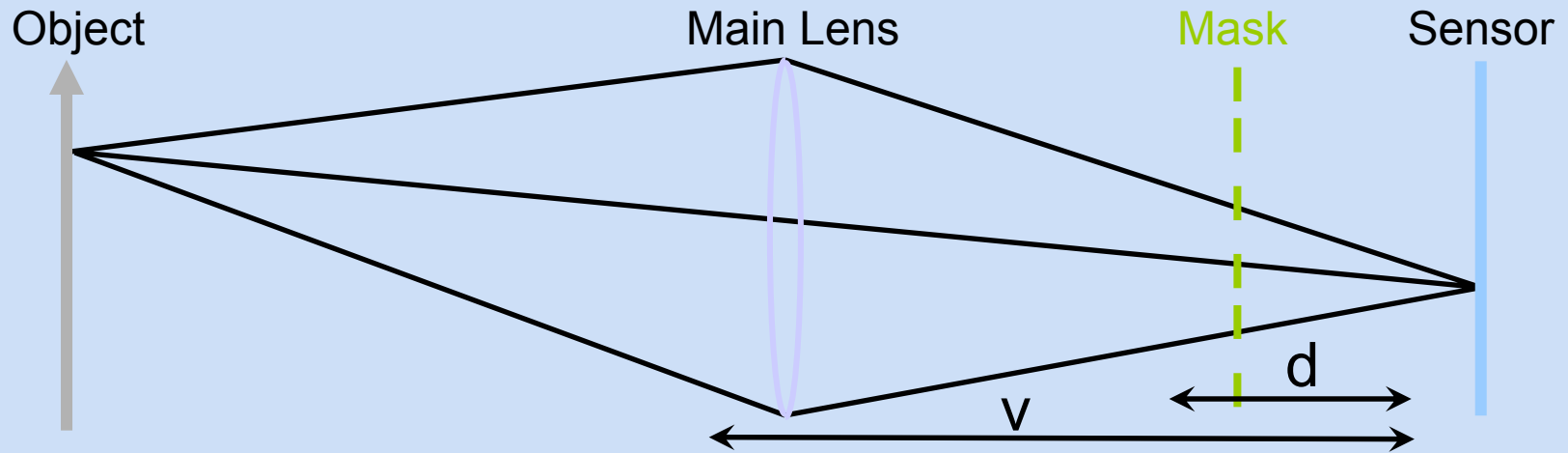
$1/f_0$

Zoom in of the  
cosine mask

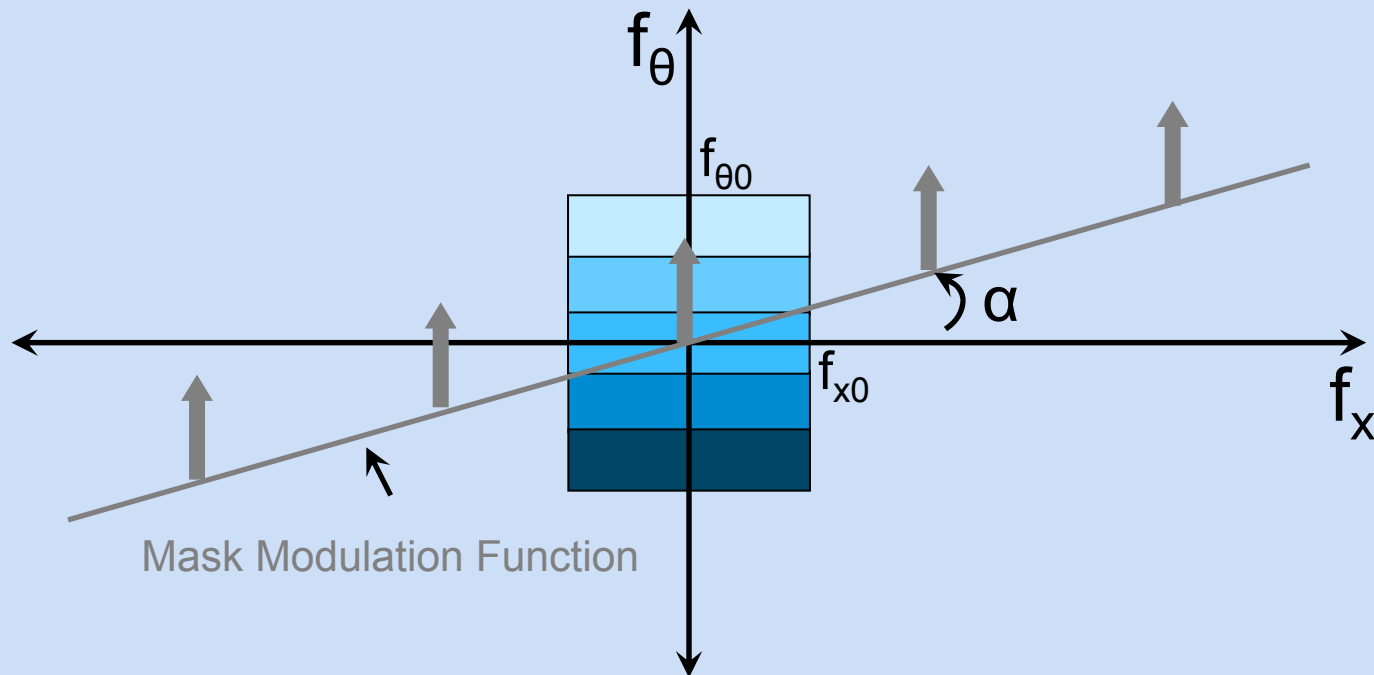


Mask is the sum of cosines with four harmonics. Plot shows the cosines. Since the physical mask cannot have negative values, a constant needs to be added.

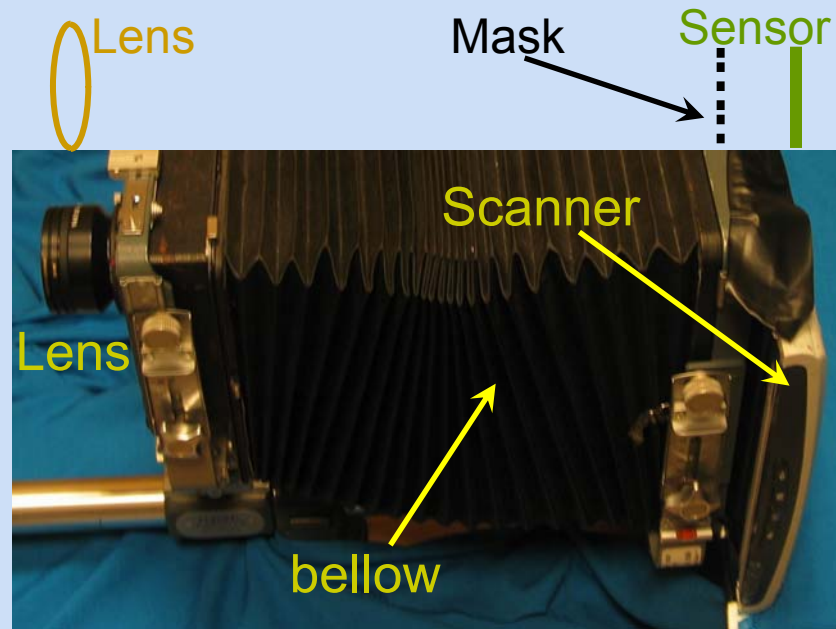
# Mask-based Heterodyning



$$\alpha = (d/v) (\pi/2)$$



# Implementation



Light Field Camera

We use Canon flatbed scanner as the sensor and Nikkor lens in front. The mask is placed is about 1 cm in front of the sensor.