Is Imitation Learning the Route to Humanoid Robots?

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Summary

This review investigates two recent developments in artificial intelligence and neural computation: learning from imitation and the development of humanoid robots. It will be postulated that the study of imitation learning offers a promising route to gain new insights into mechanisms of perceptual motor control that could ultimately lead to the creation of autonomous humanoid robots. Imitation learning focuses on three important issues: efficient motor learning, the connection between action and perception, and modular motor control in form of movement primitives. It will be reviewed how research on representations of, and functional connections between action and perception have contributed to our understanding of motor acts of other beings. The recent discovery that some areas in the primate brain are active during both movement perception and execution has provided a hypothetical neural basis of imitation. Computational approaches to imitation learning will also be described, initially from the perspective of traditional AI and robotics, but also from the perspective of neural network models and statistical learning research. Parallels and differences between biological and computational approaches to imitation will be highlighted and an overview of current projects that actually employ imitation learning for humanoid robots will be given.

In 1921 Karel Capek's play *Rossum's Universal Robots* (1) provided the first concrete vision of how a robot should look: it should look like a human being. Since this time, science fiction stories have created a never ending stream of increasingly sophisticated superhuman machines, but research has not been able to realize a robot that comes even close to Capek's relatively "simple" artificial humans. What makes it so hard to create a human-like robot? From an engineering point of view, an argument could be made that appropriate materials, motors, power supplies, and sensors are missing to achieve the compact, compliant, and lightweight design of biology. However, even if we had access to a robotic system that incorporated all these desirable properties, and even if this machine were equipped with a supercomputer, we would still not succeed in creating a humanoid. The problem is that the algorithms required to program this machine such that it achieves the versatility and flexibility of biological systems are not yet available. For the time being, robots can only solve tasks after the task has been carefully analyzed and added to the robot program by a human. An impressive example of such a procedure was recently provided by the research laboratories of the Honda Corporation in Japan (2; 3). In about 10 years of work, Honda created the first humanoid robot that can walk, climb stairs, and manipulate simple objects (Figure 1).

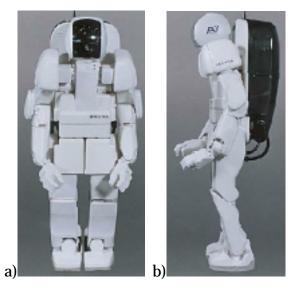


Figure 1: Honda Humanoid Robot in a) frontal, and b) side view.

However, the amount of work it took to build the Honda robot, and the fact that, besides locomotion, the machine requires teleoperation to perform other tasks, is far from satisfying.

In order to overcome the need for teleoperation and manual "hard-coding" of every behavior, a learning approach is required. The most general approach to learning control is reinforcement learning (4, 5). Reinforcement learning usually requires an unambiguous representation of states and actions of the movement system and the existence of a scalar reward function. Learning proceeds by trying actions in a particular state, and, based on the received, possibly delayed (6) reward, updating an evaluation function that assigns expected rewards to

possible actions. After learning, the action with the highest expected value in each state is chosen to achieve the task goal.

An important element of learning control is the requirement to explore new actions in order to find good, or even optimal, solutions to a given movement task. For a movement system with many degrees of freedom, there is an exponential explosion in the number of actions that can be taken in every state. For example, the Honda robot in Figure 1 has 30 degrees-of-freedom (DOFs), each of which needs a motor command at every instant in time. Even if the command for each DOF has only three possible values, e.g., forward, backward, and zero, there is a combination of $3^{30}>10^{14}$ different actions that can be taken in every state. As it is impossible to search such huge spaces for what constitutes a good action, it is necessary to either find more compact state-action representations, or to focus learning on those parts of the state-action space that are actually relevant for the movement task at hand. In the following article, we will review how the latter topic can be approached in the framework of imitation learning, while the former topic, i.e., compact state-action representations, will be shown to be a natural prerequisite for imitation learning in the form of movement primitives

Movement Imitation

Movement imitation is familiar to everybody from daily experience: a friend demonstrates a movement, and immediately we are capable of approximately repeating it. For the purpose of this review, only visually mediated imitation will be considered, although, at least in humans, verbal communication can supply important additional information. From the viewpoint of motor learning, a teacher's demonstration as the starting point of one's own learning can significantly speed up the learning process: imitation drastically reduces the size of the state-action space that needs to be explored (7). With an eye towards computational approaches, we will first review some of the most relevant milestones in the study of imitation learning before we will look into the promises and challenges that imitation learning poses to computational modelers.

Imitation from the Viewpoint of Behavioral and Cognitive Sciences

In infant and animal studies, the ability to imitate is usually concluded from the subject's increased tendency to execute a previously demonstrated behavior. However, other causes can equally account for a higher probability of the subject's behavior, in particular priming, emulation, and response facilitation (Glossary); such causes are not to be mistaken with true imitation (8, 9). True imitation is present only if i) the imitated behavior is new for the imitator, ii) the same task strategy as that of the demonstrator is employed, and iii) the same task goal is accomplished (9). For example, if a movement is not new, response facilitation rather than imitation can account for the imitator's behavior. However, as will be shown below, from a computational point of view, imitative behavior in the form of response facilitation already contains very complex problems. Thus, a formal understanding of the mechanisms of response facilitation would constitute significant scientific progress.

Behavioral and cognitive sciences have long been interested in imitation of movements, from Darwin (10) and Thorndike (11) to Piaget (12). After Piaget's work, movement imitation did not receive widespread attention anymore, partially due to the prejudice that "imitating" or "mimicking" is not an expression of higher intelligence. This attitude changed in the 1970's, to some extent due to studies of Meltzoff and Moore (13). These authors reported on the ability of 12-21 day old and, later, even less than an hour old infants (14) to imitate both facial and manual gestures. Young infants of this age had neither seen their own faces nor been exposed to viewing faces of other humans for any significant amount of time. Thus, the ability to map a perceived facial gesture to their own gestures was concluded to be innate and contradicted Piaget's ontogenetic account of imitation (12). In the light of this new interest in imitation learning, it was discovered that many animals are unable to learn by imitation (9, 15). These findings contributed to today's view of imitation as an important expression of higher intelligence. In recent years, a significant amount of new work has been published on imitation learning in humans and animals. Examples include comparative studies between human and monkey imitation (16), the interplay between memory and imitation and its implications for learning (17, 18), and the focus of attention while observing a demonstration (19). Imitation is also closely connected to research that investigates the connection between action and perception (20, 21, 22).

| Glossary |
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| <i>Accommodation</i> : The process by which an activated internal perceptual motor representation is adapted to better suit a new task. |
| <i>Action Level Imitation</i> : The indiscriminate copying of the actions of the teacher without mapping them onto more abstract motor representation. |
| <i>Action</i> : All variables (discrete or continuous) that can actively change the state of a system. Usually, actions are motor commands, abbreviated as a vector u. |
| Assimilation: The mapping of an observed behavior onto an existing perceptual motor representation. Control Policy: A function that maps the state x of a movement system and its environment into an appropriate action u for a particular task, i.e., $\mathbf{u} = p(\mathbf{x}, t, a)$. As indicated, the function π can directly depend on the time, t , and some additional parameters α that may be useful to adjust the policy for a particular task goal. Movement |
| <i>Primitives</i> can be formalized in the form of control policies. <i>Deferred Imitation</i> : Imitation that takes place a certain amount of time after the demonstration was given by the |
| teacher. |
| <i>Emulation</i> : Goals in the environment become overt due to the actions of others. Afterwards, the observer strives to attain the same goal. |
| <i>Forward Model</i> : A mathematical model that predicts the time evolution of a dynamical system. For example, differential equations of motion in the form of $\dot{\mathbf{x}} = f(\mathbf{x}, \mathbf{u})$ are prototypical forward models in motor control. <i>Immediate Imitation</i> : Imitation that takes place immediately after the demonstration of the teacher. |
| <i>Movement Primitation</i> . Initiation that takes place minediately after the demonstration of the teacher. <i>Movement Primitive</i> : A sequence of actions that can accomplish a certain movement goal. See <i>Control Policy</i> for a more formal definition. |
| <i>Object-Centered Representations</i> : The representation is insensitive to the relative position and orientation of the perceived object to one's own body. |
| <i>Priming</i> : Stimuli in the environment that co-occur with the actions of the teacher increase the observer's activa- tion of corresponding internal representations in memory. Consequently, the observer's exploratory behavior will be biased by these activations towards receiving similar stimuli. |
| <i>Program Level Imitation</i> : A process by which the structural organization of a behavior is copied from observing a teacher, while the exact details of actions are filled in by individual learning. |
| <i>Response Facilitation</i> : Observed actions enhance corresponding action representations in memory. Afterwards, it is more likely that the observer performs the observed action. |
| <i>Reward Function</i> : A function that provides a scalar (discrete or continuous) value about the goodness of an action u in a state x. |
| <i>Simultaneous Imitation</i> : Imitation that takes place concurrently with the demonstration of the teacher. <i>Spline Approximations</i> : A mathematical concept of curve fitting, usually with low-order polynomials. Complex curves need a sequence of concatenated splines for a good approximation. The points where a spline ends and a new one begins are called spline nodes. |
| <i>State</i> : All variables (discrete or continuous) that are necessary to model a system. In this article, all states of a system are compactly denoted as a vector x. |
| <i>State-Action Space</i> . The mathematical space spanned by actions u and states x jointly. Solving a movement task can be thought of as finding a path between two points in this state, the initial state and the goal state. |
| <i>Stimulus Enhancement</i> : An object or place becomes more salient due to the actions of the teacher in its vicinity or in conjunction with the object. This enhancement will draw the observer's attention or elicit responses towards this object or place. |
| <i>Supervised Learning</i> : Learning of an input to output mapping under the premise that an explicit error signal can be provided for each output. For instance, a <i>Control Policy</i> is a function that can be learned by supervised learning if both the state x and the appropriate target action u are given to the learning system. |
| Task Level Learning: Learning of a task can take place by learning an appropriate <i>Control Policy</i> that generates commands u on the actuator level, or by learning a <i>Control Policy</i> that generates commands in a more abstract but task related space, e.g., the space of the finger tip. The latter approach is called task-level learning and it requires additional transformations to map the task-level command into actuator space. Usually, errors in per- |
| formance are more associated with task commands than actuator commands. <i>Viewer-Specific Representations</i> : The representation is sensitive to the relative position and orientation of the perceived object to one's own body. |
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Behavioral studies can provide several sources of ideas for computational motor control and imitation learning. For instance, the principle of emulation is interesting for learning how to direct the focus of attention towards favorable goals, and priming can be used to bias explorative behavior towards useful stimuli. Thus, both principles help reducing the number of inputs to a motor system by focusing on important stimuli, but they do not reduce the combinatorial explosion of possible actions that can be explored in a particular state. Alternatively, Meltzoff and Moore's (23) postulate of imitation as a bootstrapping for communication may offer an interesting starting point for computational modelers. The authors argued that given a partially familiar stimulus in the environment (e.g., a face), imitating what this "stimulus" did during a previous encounter should trigger either a familiar or an unfamiliar response in how the stimulus will change. Such a strategy would help to disambiguate stimuli by acting upon them. Interestingly, we will encounter a similar interpretation of the purpose of imitation from a neurophysiological perspective, and a related computational mechanism for movement recognition based on predictive forward models in the section on neural network models to imitation. A more concrete concept of imitation was suggested in Meltzoff and Moore (24). In their 'Active Intermodal Mapping' (AIM) model, they suggest that visual perception of the teacher's movement is converted into a higher level representation that can be matched against appropriately transformed proprioceptive information about one's own movement. If this matching space is given, imitation can be seen as learning to achieve a target representation, a problem that can be tackled with techniques from supervised learning (25). This idea can be rephrased in computational terms, as will be discussed below.

Imitation from the Viewpoint of Neuroscience and Cognitive Neuroscience

An essential prerequisite for imitation is a connection between the sensory systems and the motor systems such that percepts can be mapped onto appropriate actions. This mapping is a difficult computational process as visual perception takes place in a different coordinate frame to motor control. This process is also more complex than pure object recognition since it requires integration of multiple objects (i.e., several limbs), their spatial relations, their relative and absolute movements, and even the intention of these movements. Given the current knowledge about neuroanatomy in primates, such a process is likely to happen in various steps, involving both the ventral (what) and dorsal (where, how) pathways (26) (Figure 2). From a neurophysiological point of view, a first question that can be addressed is whether there are any particular brain areas and representations that are specialized to facilitate imitation.

Perrett and co-workers (27, 28, 29) reported that neurons within the superior temporal sulcus (STs) of macaques (Figure 2) respond to both form and motion of objects. Interestingly, many cells were sensitive to movements of specific body parts of an observed human. For instance, cell specificity was found for faces with translatory motion in a particular direction, faces that rotated, movement of particular body parts (head, arm, leg, hip) and combinations of body parts, and even movement of the entire

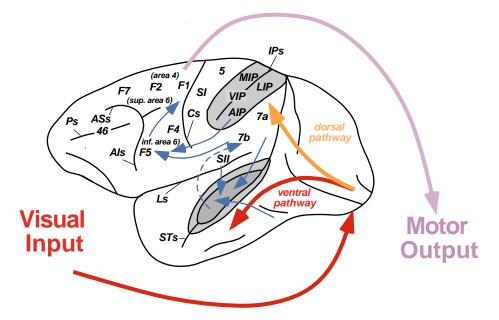


Figure 2: Sketch of a monkey brain and some areas that are hypothesized to be involved in imitation. Abbreviations denote: Ps: principle sulcus, AIs: inferior arcuate sulcus, ASs: superior arcuate sulcus, STs: superior temporal sulcus, Cs: central sulcus, Ls: lateral sulcus, IPs: intraparietal sulcus, MIP: medial intraparietal area, VIP: ventral intraparietal area, LIP: lateral intraparietal area, AIP: anterior intraparietal area, SII: secondary somatosensory cortex (adapted from Rizzolatti et al. (32) and Perrett et al. (30)). Gray areas indicate an opened sulcus. Blue arrows indicate known neuronal projections between different areas of the brain, dashed arrows indicate hypothesized connections.

body. In the lower bank of the STs, similar phenomena were found for actions of the hand (28). Two important characteristics of this distributed representation are worth highlighting. First, most cells were viewer specific, i.e., there existed no indication of an object centered representation. From this property, Perrett et al. (30) concluded that STs is well suited to extract the attention and goals of others. Second, due to a connection of somatosensory cortex to STs (Figure 2), most of the form and motion neurons were insensitive to self-motion due to re-afferent signals (31). Thus, STs neurons are in the ideal situation to analyze the movement of others without interference from one's own body and seem to be an excellent candidate for a first processing step for imitation.

What is the next processing step in a hypothesized neural pathway for imitation? Area F5 in monkeys could play a crucial role (Figure 2). Rizzolatti et al. (33) found neurons in area F5 that were specific to the execution of goal related movements, e.g., 'reaching', 'bringing-to-the-body', 'grasping-with-the-hand', as well as selective to a particular type of grasp, for instance, precision grips, finger prehension, or whole-hand-prehension. Interestingly, many neurons in F5 were active during the entire or at least extended parts of a motor act, instead of just a single submovement or muscle activation. Jeannerod et al. (34) and Murata et al. (35) interpreted this firing pattern as

coding complete segments of motor acts, or motor schemas (36). The possible connection to imitation, however, came with the finding that some of the neurons in F5, called "mirror neurons", were active *both* when the monkey *observed* a specific behavior and when it *executed* it itself (37). Mirror neurons fire highly specifically only to a special motor behavior with a particular object. These results are similar to those in STs (28), with the difference that neurons in STs do not respond to executed motor acts, but rather only to perceived ones. From imaging and transcranial magnetic stimulation studies, there is also some evidence that a similar mirror system exists in humans (38, 39, 40). Surprisingly, this system seems to involve Broca's area (41), a brain region normally only associated with speech production. The possible homology of F5 in monkey and Broca's area in humans led some authors (41) to speculate that the ability to imitate actions and to understand them could have subserved the development of communication skills. This idea is consistent with Meltzhoff and Moore's (23) developmental work and interpretations.

Whether mirror neurons are really part of the imitation system, however, has remained speculative so far. Neither did the neurophysiological experiments on mirror neurons require true imitation behavior nor did they test a movement repertoire that monkeys are known to imitate. Gallese and Goldman (42) rather suggest that mirror neurons participate in "mind reading", a process accomplished by using one's own mental apparatus to predict the psychological state of others through mental simulations. In computational approaches, mental simulations are based on predictive forward models (43). As will be discussed in the next section, forward models are likely to be an important component of an imitation learning system. From this viewpoint, simulation theory and imitation learning may share some computational mechanisms.

The connection between neurons in STs and F5, however, remains unclear at present. Area F5 does receive input from SII, 7b, and AIP (Figure 2), and sends projections to F1, i.e., primary motor cortex, the spinal cord, and also back to AIP (35). AIP neurons were shown to be either sensitive to object specific properties (shape, size, orientation) or to movements and grasps executed by the monkey, or to both visual and motor stimuli (44). Due to the additional observation that many AIP neurons were modulated during ongoing grasping movements, Jeannerod et al. (34) hypothesized that AIP may provide the necessary spatial object information to F5 for continuous guidance of grasping movement. Since AIP receives input from other parietal areas, the connection to visual information through the dorsal stream seems to be complete. However, this visual information is more concerned with object properties, rather than information about the movement of others. Arbib and Rizzolatti (45) speculate that a connection from STs to area 7b and then to F5 provides the input about the movements of others. Such statements are partially supported by imaging studies that demonstrated the simultaneous activation of the inferior area 6 and STs in humans (46, 47). The STs->7b->F5 connection would complete a first hypothesis for a neurophysiological pathway of imitation.

Imitation from the Viewpoint of Robotics, Artificial Intelligence, and Neural Computation

Symbolic Approaches to Imitation Learning

At the beginning of the 1980's, the idea of imitation learning started to find increasing attention in the field of manipulator robotics as it seemed to be a promising route to automate the tedious manual programming of robots. Inspired by the ideas of artificial intelligence, symbolic reasoning was commonly chosen to approach imitation, as outlined in the following (e.g., 48, 49, 50, 51, 52). During a training phase, several example movements were generated under manual robot control that achieved a given task with a robot. Sensor readings, e.g., position and force, were stored throughout the demonstration together with the positions and orientations of obstacles and the goal state. For imitation, the example movements were first segmented into subgoals and appropriate primitive actions to attain these subgoals. Primitive actions were commonly chosen to be the simple point-to-point movement that industrial robots employed at this time. Subgoals could be the robot's gripper orientation and position—defined in a geometrical relation to the goal—after each primitive action, or they were labeled manually by the demonstrator (50). Consequently, the demonstrated task was segmented into a sequence of state-action-state transitions. However, given some uncertainty in the environment and some variability between several demonstrated movements, it was necessary to consolidate all demonstrated movements. For this purpose, the state-action-state sequence was converted into symbolic "if-then" rules, for instance, expressing the state in terms of 'aligned', 'in contact', 'near-to', and actions as 'move-to', 'grasp-object', 'move-above', etc. Appropriate numerical definitions of these symbols, e.g., at which distance threshold an object is near, were provided as prior knowledge. Such abstraction resulted in graph-based representations, each state becoming a graph node and each action a directed link between two nodes. Symbolic reasoning could now unify different graphical representations for the same task by merging and deleting nodes (49) such that the final program for imitating the demonstrated movement was achieved.

In essence, many recent robotics approaches to imitation learning have remained closely related to the example above. New elements include to use visual input of the teacher and to perform movement segmentation out of computer vision algorithms (53; 54, 55). Other projects used data gloves (56) or marker-based observation systems as input for imitation learning (56). More recently, research on imitation learning has been influenced increasingly by non-symbolic learning tools, for instance artificial neural networks, fuzzy logic, etc. (57, 58, 59), thus entering the category of neural computation described in the following.

Inductive Approaches to Imitation Learning

Figure 3 sketches the major ingredients of an imitation learning system. Most research projects have either focused on the perceptual side of imitation by investigating movement systems with low complexity (54, 60, 61) (e.g., artificial oculomotor systems,

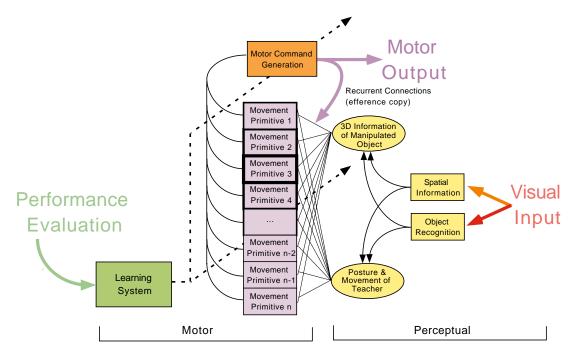


Figure 3: Conceptual sketch of an imitation learning system. The right side of the figure contains primarily perceptual elements and indicates how visual information is transformed into spatial and object information. The left side focuses on motor elements, illustrating how a set of movement primitives competes for a demonstrated behavior. Motor commands are generated from input of the most appropriate primitive. Learning can adjust both movement primitives and the motor command generator. The color of arrows matches those in Figure 2 when possible.

mobile robots, pick-and-place industrial robots), or on the motor end by assuming the existence of all necessary perceptual information. In the following, we will primarily focus on projects employing the latter strategy.

After spatial information about the teacher's movement and object information has been extracted, one of the major questions becomes how such information should be converted into action. For this purpose, Figure 3 alludes to the concept of movement primitives (Glossary), also called 'movement schemas', 'basis behaviors', 'units of action', 'macro actions', etc. (36, 62, 63). Movement primitives are sequences of action that accomplish a complete goal-directed behavior. A movement primitive can be as simple as an elementary action in the symbolic approaches to imitation, e.g., 'go forward', go backward', etc. However, as discussed in the introduction of this review, such low-level representations do not scale well to learning in systems with many degrees-of-freedom. Thus, it is useful for a movement primitive to code complete temporal behaviors, like 'grasping a cup', 'walking', 'a tennis serve', etc. This coding results in a compact state-action representation where only a few parameters need to be adjusted for a specific goal. For instance, in reaching movements, the target state and movement duration are such parameters, or in a rhythmic movement, frequency and amplitude need to be specified (64). Using such primitives dramatically reduces the number of parameters that need to be learned for a particular movement. The drawback is that the possible movement repertoire becomes more restricted.

In Figure 3, the perceived action of the teacher is mapped onto a set of existing primitives in an assimilation phase, similarly as in Demiris and Hayes (65). Subsequently, the most appropriate primitives are adjusted by learning to improve the performance in an accommodation phase. Figure 3 indicates such a process by highlighting the better-matching primitives with increasing line widths. If no existing primitive is a good match for the observed behavior, a new primitive must to be generated. This concept of movement primitives is closely related to the interpretation of mirror neurons in the previous section: mirror neurons are thought to code complete motor acts, i.e., primitives. However, mirror neurons seem to be a more high-level indicator of which movement primitive is appropriate rather than directly the place of motor command generation. Movement primitives could also form the 'supramodal' representation system of Meltzoff and Moore (24) in which the authors assume that matching between the perceived and one's own movement takes place. The authors suggested that in early infancy, matching is based on goal states for the motor system, while, at a higher developmental stage, matching may be based on a temporal sequence of goal states, or a transition between goal states. Goal states are some of the natural parameters of a movement primitive (64), and transitions between goal states are the primitive's spatio-temporal signature to which Meltzoff and Moore appeal as a candidate to achieve matching between different modes of sensory information.

Figure 3 also allows distinguishing true imitation vs. response facilitation. For explaining response facilitation, every movement primitive has to keep a frequency count of its past activations over a restricted temporal window. A demonstration of a familiar movement primitive by a teacher will change this frequency distribution, i.e., it will be biased towards the observed primitive. If spontaneous action is generated according to the probability distribution that is formed by the frequency counts, the demonstrated behavior is more likely to occur. The described process can readily be modeled by using Bayesian statistics (25). For true imitation, no existing primitive is a good match for the demonstrated behavior such that learning is required to either adapt an existing primitive or to generate a new one. From this viewpoint, response facilitation and true imitation share largely the same circuitry and have to tackle similar computational problems.

Imitation Learning of Novel Behaviors

Several research projects have focussed on imitation as a method of creating novel behaviors. Three major approaches can be distinguished.

Learning a Control Policy Directly

The demonstrated behavior can be used to learn the appropriate control policy (Glossary) directly by supervised learning. For this purpose, the state \mathbf{x} and the action \mathbf{u} of the teacher need to be observable and identifiable. This prerequisite, shared by all forms of imitation learning, imposes a serious constraint since, normally, motor com-

mands and the internal variables of the teacher are hidden from the observer. Thus, a movement primitive needs to be defined in coordinate frame based on variables that can be perceived, e.g., the acceleration of the finger tip in the task of pole balancing instead of the commands sent to the motor neurons. Aboaf et al. (66) called such an approach task-level learning, and in analogy, "task-level imitation" can be used in the context of imitation learning (Glossary). Task-level imitation requires prior knowledge of how a task-level command (e.g., the desired acceleration of the fingertip) can be converted into an actuator-level command. Motor control needs to be modular for this purpose, i.e., at least separate processes for movement planning and execution need to be assumed (67, 68).

Direct policy learning was conducted for the task of pole balancing with a computer-simulated pole (69,70). For this purpose, a neural network was trained on tasklevel data recorded from a human demonstration. Similarly, several mobile robotics groups adopted imitation by direct policy learning using a "robot teacher" (60, 71, 72, 73). For example, the "robot student" followed the "robot teacher's" movements in a specific environment, mimicked its actions, and learned to associate which action to choose in which state. Afterwards, the robot student had the same competence as the teacher in this environment. Importantly, in all these direct policy learning approaches, there is no need for the student to know the goal of the teacher. Imitation learning is greatly simplified in this manner. However, the student will not be able to undergo self-improvement unless an explicit reward signal, usually generated from an optimization criterion, is provided to the student, as in the following approaches.

Learning From Demonstrated Trajectories

A second approach to learning novel behaviors is based on building policies out of demonstrated trajectories. This idea was explored with an anthropomorphic robot arm for dynamic manipulation tasks, for instance, learning a tennis forehand and the game of kendama ('ball-in-the-cup') (74, 75). At the outset, a human demonstrated the task, and his/her movement was recorded with marker-based optical recording equipment. This process resulted in data about the movement of the manipulated object in Cartesian coordinates, as well as the movement of the actuator (arm) in terms of joint angle coordinates. For imitation learning, a hybrid strategy was chosen. Initially, the robot aimed at indiscriminate imitation in task space based on position data of the endeffector, while trying to use an arm posture as similar as possible to the demonstrated posture of the teacher. Afterwards, based on manually provided knowledge of the task goal in form of an optimization criterion, the robot's performance improved by trial and error learning until the task was accomplished. For this purpose, the desired endeffector trajectory of the robot was approximated by splines, and the spline nodes, called via-points, were adjusted by supervised learning until the task was fulfilled. Using this method, the robot learned to manipulate a stochastic, dynamic environment within a few trials.

Model-based Imitation Learning

Outstanding Questions

• *Learning perceptual representations.* How can appropriate representations of the identity and movement of others be developed in an automated fashion from visual input? Is it necessary that such representations develop simultaneously with the motor representations?

• *Movement primitives*: Is there a basic set of primitives that can initialize imitation learning? How complex are the most elementary primitives in this set? How can new primitives be learned, and old primitives be combined to form higher level movement primitives? How is sequencing and the recognition of sequences of movement primitives accomplished?

• *Movement recognition through movement generation*: Is the movement generating mechanism directly employed for movement recognition? What representation allows such a dual use of the motor system? Are movement primitives simultaneously predictive forwards models?

• *Understanding task goals:* How can the intention of a demonstrated movement be recognized and converted to the imitator's goal?

A third approach to learning a novel primitive employs model-based learning (76, 7). From the demonstrated behavior, the dynamics of the task is approximated in the form of a predictive forward model (cf. 77). Given knowledge of the task goal, the task-level policy of the movement primitive can be computed with reinforcement learning procedures based on the learned model. For example, Schaal and Atkeson (76, 78) showed how the modelbased approach allowed an anthropomorphic robot arm to learn the task of pole-balancing in just a single trial, and the task of a "pendulum swing-up" in only three to four trials. These authors also demonstrated that task-level imitation based on direct policy learning, augmented with subsequent self-

learning, can be rather fragile and does not necessarily provide significant learning speed improvement over pure trial-and-error learning without a demonstration.

Implications for Computational Models of Imitation Learning

The approaches discussed in the previous paragraphs illustrated some computational ideas for how novel behaviors can be learned by imitation. Interesting insights into these methods can be gained by analyzing the process of how a perceived behavior is mapped onto a set of existing primitives. Two major questions (24) become a) what is the matching criterion for recognizing a behavior, and b) in which coordinate frame does matching take place?

If only the control policy of the movement primitive exists, finding a matching criterion becomes difficult. One solution would be to try a primitive, observe its outcome in task space, and generate a performance criterion based on the similarity between the executed and the teacher's behavior. This procedure needs to be repeated for every primitive in the repertoire and is thus quite inefficient. Another possibility arises if the primitive outputs task-level commands that can be compared directly with the teacher's performance. In this case, the movement primitive acts simultaneously as a forward model (64), an approach that is described in more detail below.

The via-point method (74) can easily be adapted for movement recognition. Viapoints are a parsimonious representation of a movement and may be used for classification as well. For example, a demonstrated movement can be transformed into viapoints, and the number and location of via-points can be compared against those of existing movement primitives in order to choose the best match, as has been demonstrated for handwriting and character recognition (79). Despite the fact that there are various open issues with regard to translation, scale, and rotation invariance in the via-point approach, the suggested bidirectional interaction between perception and action is noteworthy. Movement recognition is directly accomplished with the movement generating mechanism. This concept is compatible with what has been observed in mirror neurons, and it also ties into other research projects that emphasize the bidirectional interaction of generative and recognition models (80) in unsupervised learning.

Lastly, a third alternative should be considered, based on forward models (76, 7), but put into a multiple-model competition (68, 81, 65). If every movement primitive has a forward model, all primitives can simultaneously attempt to predict the teacher's behavior in the form of a mental simulation loop, indicated by the 'efference copy' arc in Figure 3. The motor command will be generated by the primitives that make the most accurate prediction. As in the via-point approach, movement recognition is based on the movement generating mechanism, as, for instance, in Wolpert and Kawato (68) and Demiris and Hayes (65). Such an approach is particularly easy if movement primitives are coded in task space since the prediction of a primitive will be directly comparable to the teacher's performance. If the primitive operates in actuator space, additional coordinate transformations are needed before a task level comparison can be accomplished (68). Since forward models have various additional advantages for motor control (43, 68), movement recognition based on forward models could offer the most general and powerful solution to the perception to action mapping. Interestingly, movement recognition based on forward models integrates smoothly with the simulation theory of mind reading (42). It can also provide a computational mechanism for Meltzoff and Moore's (23; 24) ideas of imitation as a basic communication skill and their 'Active Intramodal Matching" model of imitation.

One final issue concerns the imitation of complex motor acts that involve learning a sequence of primitives and when to switch between them. In this context, Fagg and Arbib (82) provided a model of reaching and grasping based on the known anatomy of the fronto-parietal circuits, including the mirror neuron system. Essentially, their model employed a recurrent neural network that sequenced and switched between motor schemas based on sensory cues. In a robotic study, Pook and Ballard (58) used hidden Markov models to learn appropriate sequencing from demonstrated behavior. There is also large body of literature in the field of time series segmentation (83, 84, 85) that employed competitive learning and forward models for recognition and sequencing in a way that is easily adapted for imitation learning as illustrated in Figure 3.

Is Imitation Learning the Route to Humanoid Robots?

In the introduction of this article, we appealed to a pragmatic view of imitation learning as a means to speed up learning in complex high dimensional motor systems, such



Figure 4: Humanoid robot at the Dynamic Brain Project at the ATR Labs in Japan

as humanoid robots. This view emerged from the lack of theories of motor learning that are able to work efficiently in high dimensional spaces. Interestingly, the apparently simple idea of imitation opened a Pandora's box of important computational questions in perceptual motor control. None of the approaches described in this article could provide satisfying answers to questions of appropriate perceptual representations for imitation, motor representations, and the learning of these representations. However, consensus may be reached that research into imitation needs to include a theory of motor learning, of compact state-action representations or movement primitives, and of the interaction of perception and action. It is likely that these three components cannot be studied in isolation: perceptual representations serve motor representations, motor representations facilitate perception, and learning provides the mutual constraints between them. Learning theories based on such reciprocal interactions are currently under investigation in computational neuroscience (80, 86). On this view, instead of being an idiosyncratic research topic, imitation learning could be conceived of as a research strategy that channels investigations in computational motor control towards the im-

portant topic of action-perception coupling.

While it seems fair to say that a formal understanding of imitation would certainly be a major step towards creating humanoid robots, biomimetic robotic systems, in particular humanoid robots, have also become a new tool to investigate cognitive and biological questions (87). For instance, the Cog project at the Massachusetts Institute of Technology investigates how far a humanoid robot could become "cognitive" via a bottom-up approach (88). The Dynamic Brain Project at the ATR Laboratories in Japan has been conducting research with an anthropomorphic robot arm for several years (74, 76) and is currently working with a novel humanoid robot (Figure 4) to study theories of computational neuroscience and imitation learning. Other humanoid robot projects include a research group at the University of Tokyo (89), and the humanoid robotics project at Waseda University (90). The blending of psychology, neuroscience, and engineering in such research projects seems to be a new trend that will be beneficial for advancing knowledge in both technological and biological sciences.

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